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Chapter 9

Inferences Based on Two Samples

- 9.1 z-Tests
- 9.2 The Two-Sample t-Test
- 9.4 Difference Between Population Proportions
- 9.5 Two-Population Variances

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Summary for $H_0: \mu_1 - \mu_2 = \Delta_0$

Test statistic value:
$$z = \frac{\bar{x} - \bar{y} - \Delta_0}{\sqrt{\frac{\sigma_1^2}{m} + \frac{\sigma_2^2}{n}}}$$

- $H_a: \mu_1 - \mu_2 > \Delta_0$ reject when $z \geq z_\alpha$ (**upper-tailed test**)
- $H_a: \mu_1 - \mu_2 < \Delta_0$ reject when $z \leq -z_\alpha$ (**lower-tailed test**)
- $H_a: \mu_1 - \mu_2 \neq \Delta_0$ reject when $z \geq z_{\alpha/2}$ or $z \leq -z_{\alpha/2}$ (**two-tailed test**)

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Example

Analysis of a random sample consisting of 20 specimens of cold-rolled steel to determine yield strengths resulted in a sample average strength of 29.8 ksi. A second random sample of 25 two-sided galvanized steel specimens gave a sample average strength of 34.7 ksi.

Assuming that the two yield-strength distributions are normal with standard deviations 4 and 5, respectively, does the data indicate the corresponding true average yield strengths are different? Use significance level 0.01.

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