You have 50 minutes to complete this test. You must *show all work* to receive full credit. Work any 6 of the following 7 problems. Clearly **CROSS OUT** the problem you do not wish me to grade. Each problem is worth 16 points, and you get 4 points for free, for a total of 100 points. The answers will be posted on the electronic reserves later today.

1. Find the area of the region bounded by the curves $y = x^2$ and $y = 2x - x^2$. Be sure to sketch a graph first!

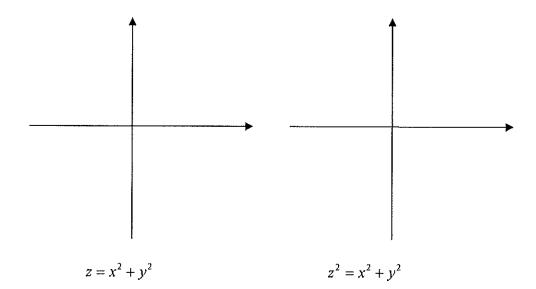
2. For $f(x, y, z) = x^2 y^3 - \frac{x}{z} + e^x \ln y$, find f_x , f_y , and f_z .

3. Find and classify the critical points of $f(x, y) = -x^4 + 4xy - 2y^2 + 1$.

- 4. Suppose p_1 and p_2 are the prices of two products. Also suppose $D_1(p_1, p_2) = 500 0.5p_1 p_2^2$ and $D_2(p_1, p_2) = 10,000 8p_1 100p_2^2$ are the demand functions for the two products (quantities). Answer the following questions, showing your work below.
 - a) Are these two products competitive (substitutes), complementary, or neither?

b) An example of two products that might behave this way are _____ and ____ .

5. Sketch at least three level curves for $z = x^2 + y^2$ on the first set of axes below. Then sketch at least three level curves for $z^2 = x^2 + y^2$ on the second set of axes. Describe the three dimensional surface represented by each and why you think each surface has that shape based on your level curves.



6. Calculate $\int_0^\infty \frac{x}{\left(x^2 + 5\right)^2} dx$.

Suppose a manufacturing firm has budgeted \$60,000 per month for labor and materials. If \$x\$ thousand is spent on labor and \$y\$ thousand is spent on materials, and if the monthly output (in units) is given by N(x, y) = 4xy - 8x, how should the budget be allocated in order to maximize the output N? What is the maximum output?