Math 15, Exam 4, Apr 26, 2007

Instructions

Calculators may be used on this exam.

However, you must show your work in order to receive credit.

- 1. Be sure to print your name and your instructor's name in the space provided.
- 2. Work all problems. Show all work. Full credit will be given only if work is shown which fully justifies your answer.
- 3. There will be sufficient space under each problem in which to show your work.
- 4. If there is a box provided, the final answer must be placed in there according to the instructions. Otherwise, box your final answer. *All final answers must be simplified!*
- 5. This exam has 3 sheets of paper (front and back). Do not remove the staple! There are 100 points. Each problem is 10 points.
- 6. Turn off your cell phone if you have one with you.

Get ready for the exam

- 1. Some formulas will be supplied (see below). You are asked to remember other formulas and techniques from Chapters 7-12 and Math 14.
- 2. You should be able to do all of the following:
 - a. Do calculus with hyperbolic functions.
 - b. Use the midpoint, trapezoidal, and Simpson rules.
 - c. Find the length of an arc and the surface area of rotating objects.
 - d. Calculate force due to liquid pressure and find the centroid of a planar figure.
 - e. Check whether a given function is a pdf, find the mean and related probabilities.
 - f. Check whether certain functions are solutions of given differential equations.
 - g. Solve problems of exponential growth or decay such as bacteria growth, radioactive decay, Newton's law of cooling, and continuously compounded interest.
 - h. Sketch curves given in parametric form.
 - i. Do calculus with parametric curves.



$$S_n = \frac{\Delta x}{3} \left[f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \dots + 2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n) \right]$$

$$T_n = \frac{\Delta x}{2} \left[f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n) \right]$$

$$\begin{split} M_y &= \rho \int_a^b x [f(x) - g(x)] dx \qquad M_x = \rho \int_a^b \frac{1}{2} \left[(f(x))^2 - (g(x))^2 \right] dx \\ \bar{x} &= \frac{M_y}{m} \qquad \bar{y} = \frac{M_x}{m} \qquad m = \rho A \\ L &= \int_a^b \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx \qquad L = \int_a^d \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy \end{split}$$