1. Solve the initial value problem $ty' + 3y = t^2$, $y(1) = 0$.
2. Given are two tanks containing 3 gallons of water each. At time 0, the first tank contains 1 lb of dye thoroughly mixed, and there is no dye in the second tank. Now, water is entering the first tank at a rate of 3 gallons per minute. From the first tank water is flowing into the second tank at a rate of 3 gallons per minute. And water is leaving the second tank, also at a rate of 3 gallons per minute. Determine the amount of dye in the first tank at time t and determine the amount of dye in the second tank at time t.
3. Find all real solutions of $y'' - 2y' + 2y = \mathrm{e}^t$ using (a) the methods of Chapter 3 and (b) the methods of Chapter 6.
4. A mass weighing 8 lb stretches a spring 6 inches. At time 0 the mass is released from a point 5 inches below the equilibrium position with upward velocity of 8 ft/sec. Determine the function which describes the subsequent free motion of the mass (ignoring any damped forces), find the period, frequency, and amplitude of the motion, and draw a picture.
5. Solve the initial value problem $P_{n+2} = \frac{2}{3}P_{n+1} + \frac{2}{9}P_n$, $P_0 = P_1 = 1$.
6. Find the first five terms of a series solution about $x_0 = -1$ for $y'' - xy' - y = 0$, $y(0) = y'(0) = 1$.
7. Use Laplace transforms to solve $y'' + 3y' + 2y = \delta(t-5) + u_{10}(t)$, $y(0) = 0$, $y'(0) = 1/2$.
8. Find the general solution of $x' = \begin{pmatrix} 5 & -1 \\ 3 & 1 \end{pmatrix} x$.