

30. Work on problems 1–8 of Section 2.7 in the textbook.
31. Define a relation on  $\mathbb{Z}$  by  $m \sim n$  iff 7 divides  $m - n$ . Show that  $\sim$  is an equivalence relation. Find all equivalence classes.
32. Work on problems 1–5, 26, 36, 56, 58, 89–95 of Section 2.8 in the textbook.
33. Let  $f, g : \mathbb{N} \rightarrow \mathbb{N}$  be defined by  $f(n) = n^2$  and  $g(n) = 3n + 2$ . Is  $f$  one-to-one, onto, invertible? Find  $f(\{8, 9, 11\})$ ,  $g^{-1}(\{8, 9, 11\})$ ,  $(g \circ f)(4)$ ,  $(g \circ f)^{-1}(\{13, 14\})$ , and  $\mathcal{P}(f^{-1}([3, 10] \cap \mathbb{Z}))$ .
34. Let  $X = \{x_1, x_2, x_3, x_4\}$ ,  $Y = \{y_1, y_2, y_3, y_4\}$ ,  $Z = \{z_1, z_2, z_3\}$ , and define  $f : X \rightarrow Y$ ,  $g : Y \rightarrow Z$ ,  $h : Z \rightarrow X$  by  $f(x_1) = y_1$ ,  $f(x_2) = y_3$ ,  $f(x_3) = y_4$ ,  $f(x_4) = y_2$ ,  $g(y_1) = z_1$ ,  $g(y_2) = z_1$ ,  $g(y_3) = z_3$ ,  $g(y_4) = z_2$ ,  $h(z_1) = x_1$ ,  $h(z_2) = x_2$ , and  $h(z_3) = x_4$ .
- (a) Find  $h \circ g$ ,  $g \circ f$ , and  $h \circ g \circ f$ .
- (b) Find  $g(\{y_1, y_3\})$ ,  $h(Z)$ ,  $f^{-1}(\{y_1, y_3\})$ , and  $h^{-1}(\{x_3, x_4\})$ .
- (c) Is  $f$  one-to-one, onto, or invertible? How about  $g$  and  $h$ ? Find the inverse functions of whatever functions are invertible.
- (d) Find  $(h \circ g \circ f)(X) \cap \{x_2, x_3, x_4\}$ ,  $h^{-1}(X) \cup g(Y)$ ,  $Z \setminus g(Y)$ , and  $\mathcal{P}(h(Z))$ .