

Name: Solution September 20, 2023

Total Score: 120 /120

$$x = x_i + v_{ix}\Delta t + \frac{1}{2} a_x(\Delta t)^2$$

$$v_x = v_{ix} + a_x\Delta t$$

$$v_x^2 = v_{ix}^2 + 2 a_x(x - x_i)$$

$$y = y_i + v_{iy}\Delta t + \frac{1}{2} a_y(\Delta t)^2$$

$$v_y = v_{iy} + a_y\Delta t$$

$$v_y^2 = v_{iy}^2 + 2 a_y(y - y_i)$$

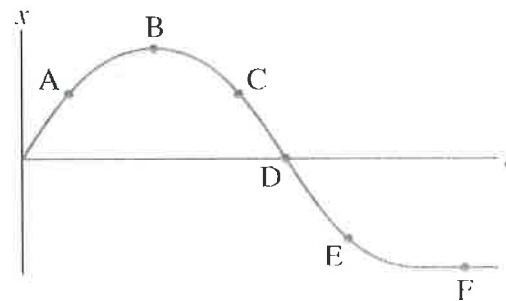
Free fall acceleration: $g = 9.8\text{m/s}^2$

Centripetal acceleration: $a_c = \frac{v^2}{R}$

$$v = \frac{2\pi R}{T}$$

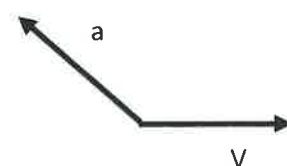
B 1.(5) The motion of an object is described by the x - t -diagram at the right. Which of the following is **true**?

- A) The object moves to the left at A.
- B) The object stops at B.
- C) The object moves to the right at C.
- D) The object stops at D.



D 2. (5) A particle is moving with velocity V . At a particular instant, it experiences an acceleration a as shown in the figure. We know that the particle is:

- A) only speeding up
- B) speeding up and changing direction of motion.
- C) only slowing down
- D) slowing down and changing direction of motion



B 3. (5) A ball is kicked from the ground with an initial velocity V at 37° above the horizontal. It travels some distance and hits a wall at some height H above the ground. Which of the following is true about the ball at the instant just before it hits the wall?

- A) Its speed is larger than the initial speed.
- B) Its speed is smaller than the initial speed.
- C) The magnitude of its acceleration is larger than the initial one.
- D) The magnitude of its acceleration is smaller than the initial one

B 4. (5) A particle is moving in a circle with constant speed. The acceleration is

- A) zero
- B) towards the center of the circle
- C) tangent to the circle
- D) away from the center of the circle

A 5. (5) A particle rotates in a circle with centripetal acceleration a . If the period is doubled without changing the radius, the new acceleration will be

- A) $\frac{1}{4} a$
- B) $\frac{1}{2} a$
- C) $2 a$
- D) $4 a$

$$T \rightarrow 2T$$

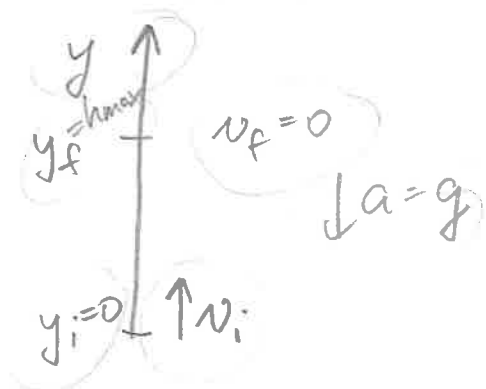
$$v \rightarrow \frac{1}{2}v$$

$$a \rightarrow \frac{1}{4}a$$

____/25 points for this page

7.(30) A child throws a ball vertically upwards at an initial speed $V_i=5$ m/s.

a) (5) In the space provided, draw a complete diagram for the ball with all information needed to solve the tasks below. Remember, any quantity used in the calculation must be defined in the diagram.



6

b) (10) Find the time ΔT the ball takes to reach the highest point. Derive a symbolic expression and calculate a numerical answer.

$$v_y^0 = v_{iy} + a_y \Delta t$$

$$0 = v_i - g \Delta t$$

$$\Delta t = \frac{v_i}{g}$$

$$\Delta t = \frac{5 \text{ m/s}}{9.8 \text{ m/s}^2} = 0.51 \text{ s}$$

c) (10) Find the height of the highest point above the launch point. Derive a symbolic expression and calculate a numerical answer.

$$v_y^2 = v_{iy}^2 + 2a_y (y - y_i)$$

$$0 = v_i^2 + 2(-g) h_{\text{max}}$$

$$h_{\text{max}} = \frac{v_i^2}{2g} = \frac{(5 \text{ m/s})^2}{2 \cdot 9.8 \text{ m/s}^2} = 1.27 \text{ m}$$

or $y = y_i + v_{iy} \Delta t + \frac{1}{2} a_y (\Delta t)^2$
 $h_{\text{max}} = v_i \left(\frac{v_i}{g} \right) + \frac{1}{2} (-g) \left(\frac{v_i}{g} \right)^2$
 same

d) (5) How big are the ball's velocity and acceleration at the highest point?

$$v_f = 0$$

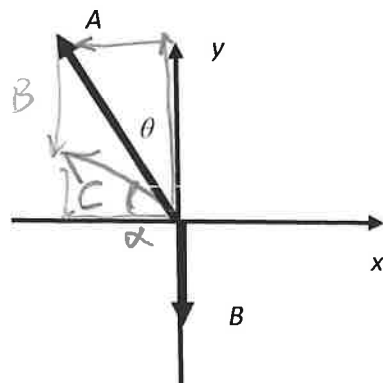
$$a_{fy} = -g$$

4

30/30 points for this page

8. (25) In the figure, the magnitudes of the vectors are $A=6$ and $B=3$. The angle θ equals 30° .

a) Calculate the vector components A_x , A_y , B_x , B_y .



$$A_x = -A \sin \theta = -6 \cdot \sin 30^\circ = -3$$

$$A_y = A \cos \theta = 6 \cdot \cos 30^\circ = 5.2$$

$$B_x = 0$$

$$B_y = -B = -3$$

b) The vector $\vec{C} = \vec{A} + \vec{B}$. Sketch vector \vec{C} in the diagram and calculate its components, magnitude, and direction.

$$C_x = A_x + B_x = -3 + 0 = -3$$

$$C_y = A_y + B_y = 5.2 + (-3) = 2.2$$

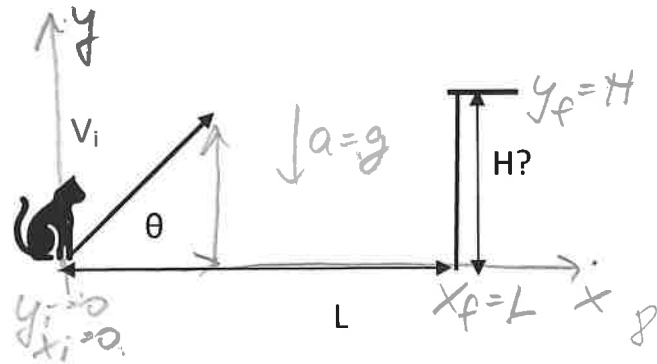
$$C = \sqrt{C_x^2 + C_y^2} = \sqrt{(-3)^2 + (2.2)^2} = 3.72$$

$$\tan \alpha = \left| \frac{C_y}{C_x} \right| \quad \alpha = \arctan \left| \frac{2.2}{-3} \right| = 36.2^\circ$$

$$\text{or } \beta = 53.7^\circ \text{ from the } y\text{-axis}$$

25 / 25 points for this page

9. (40) Raisin the cat jumps off the floor with an initial velocity of magnitude V_i directed at an angle θ with respect to the horizontal and lands on the platform of her cat tree a horizontal distance L away.



a) Complete the diagram on the right with all information necessary to solve the parts below.

b) Derive a symbolic expression for the time Δt it takes Raisin to reach the platform, in terms of V_i , L , θ and g (or a subset thereof).

$$x = x_i^0 + v_{ix} \Delta t + \frac{1}{2} a_x (\Delta t)^2$$

$$L = v_i \cos \theta \Delta t$$

$$\Delta t = \frac{L}{v_i \cos \theta}$$

c) Derive a symbolic expression for the height H of the platform, in terms of V_i , θ and g , and Δt from part b).

$$y = y_i^0 + v_{iy} \Delta t + \frac{1}{2} a_y (\Delta t)^2$$

$$H = v_i \sin \theta \Delta t + \frac{1}{2} (-g) (\Delta t)^2$$

d) What is the x-component of Raisin's velocity when she reaches the platform?

$$v_x = v_{ix} + a_x \Delta t$$

$$v_x = v_i \cos \theta$$

40/40 points for this page