

1. Suppose a snowball has radius  $r_0$  at time 0. As time goes by, the volume of the snowball is decreasing proportionally to its surface area. Find the radius  $r(t)$  of the snowball at time  $t > 0$ . (Hint: A ball of radius  $r$  has volume  $\frac{4}{3}\pi r^3$  and surface area  $4\pi r^2$ .)
2. Solve the initial value problem  $y' - 3t^2y = t^2$ ,  $y(0) = 1$ .
3. Given are two tanks containing 50 gallons of water each. At time 0, the first tank contains 1 lb of dye thoroughly mixed, and there is no dye in the second tank. Now, water is entering the first tank at a rate of 5 gallons per minute. From the first tank water is flowing into the second tank at a rate of 5 gallons per minute. And water is leaving the second tank, also at a rate of 5 gallons per minute.
  - (a) Draw a picture.
  - (b) Determine the amount of dye in the first tank at time  $t$ .
  - (c) Determine the amount of dye in the second tank at time  $t$ .
4. Separate the variables to solve the initial value problem  $P' = 2P - 2tP$ ,  $P(0) = 5$ .
5. In 1920, R. Pearl used experiments to show that the rate of change in a population of the fruit fly “drosophila” is equal to  $\frac{1}{5}P(t) - \frac{1}{5175}P^2(t)$ , where  $P(t)$  is the quantity of the population after  $t$  days. Assume that we have 10 flies at time 0.
  - (a) Find  $P(t)$  for  $t > 0$ .
  - (b) How many flies are there after 12 days?
  - (c) Find the limit of  $P(t)$  as  $t \rightarrow \infty$  and give an interpretation of your result.