

1. For the system given in Figure 1, determine  $F_1(s)$ ,  $f_1(t)$  and  $F_2(s)$ . (25pts.)

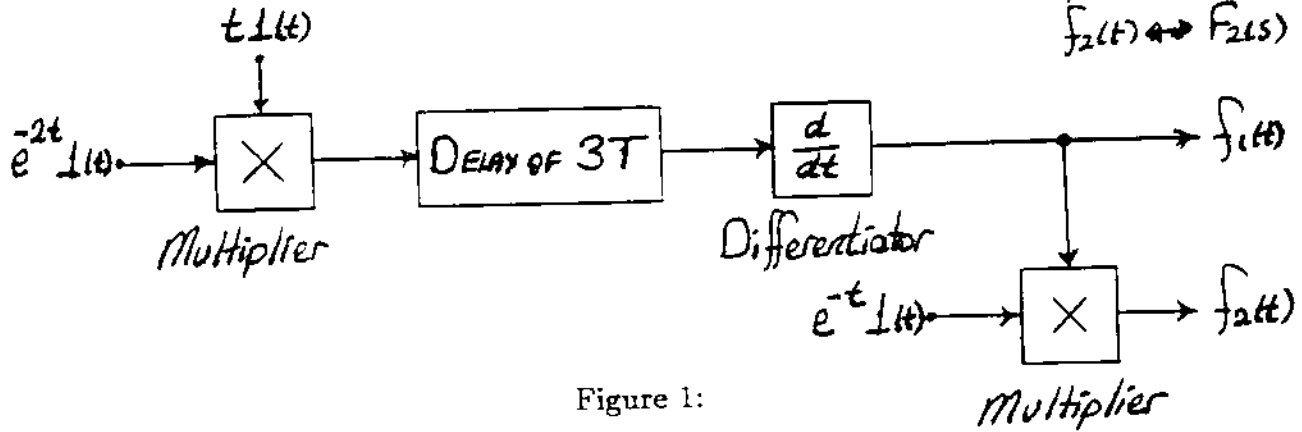


Figure 1:

2. Figure 2 shows a mechanical system. Find the differential equations describing the motion of  $m_1$  and  $m_2$  and force-voltage or force-current electric circuit analog of the system. (15pts.)

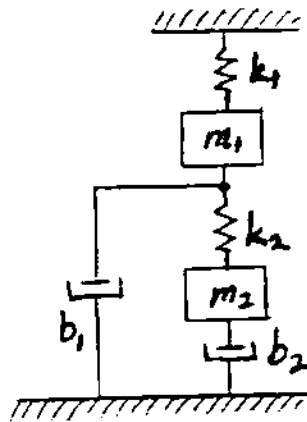


Figure 2:

3. Figure 3 shows a speed control system. The load consists of  $I$ ,  $b$  and an external torque  $\tau_L$ . The DC tachometer gives an output voltage  $v_t$  proportional to the output speed  $\omega$ . This voltage is subtracted from the reference voltage  $v_r$ , creating the difference signal  $v$ . The signal  $v$  is amplified and used to control  $i_a$ , so that the motor acquires the desired speed. Write the individual equations describing the system and form a detailed block diagram of the system using these equations. (15pts.)

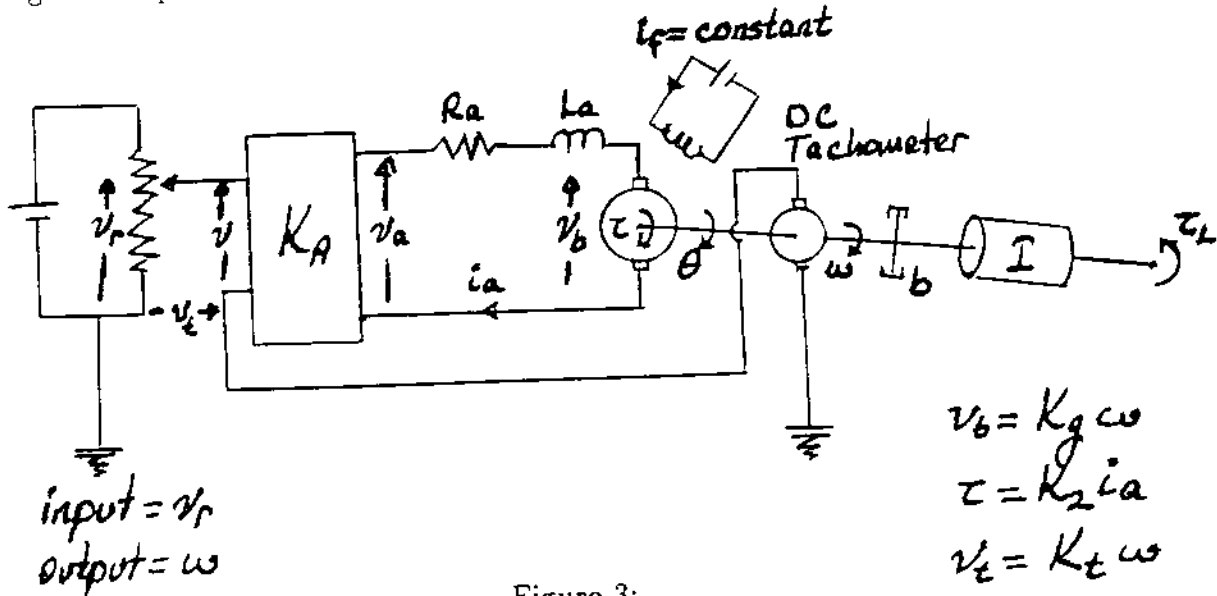


Figure 3:

4. Determine the transfer function of the system in Figure 4 by block diagram reduction. (25pts.)  
 Note: Solution with signal flow graph will only get 10 pts.

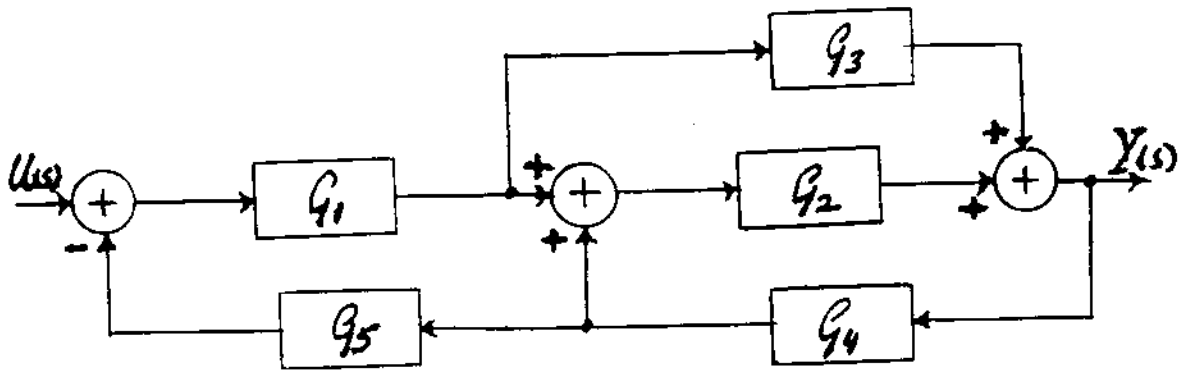


Figure 4:

5. Determine the transfer function  $C(s)/R(s)$  for the signal flow graph shown in Figure 5 using Mason's formula. (20pts.)

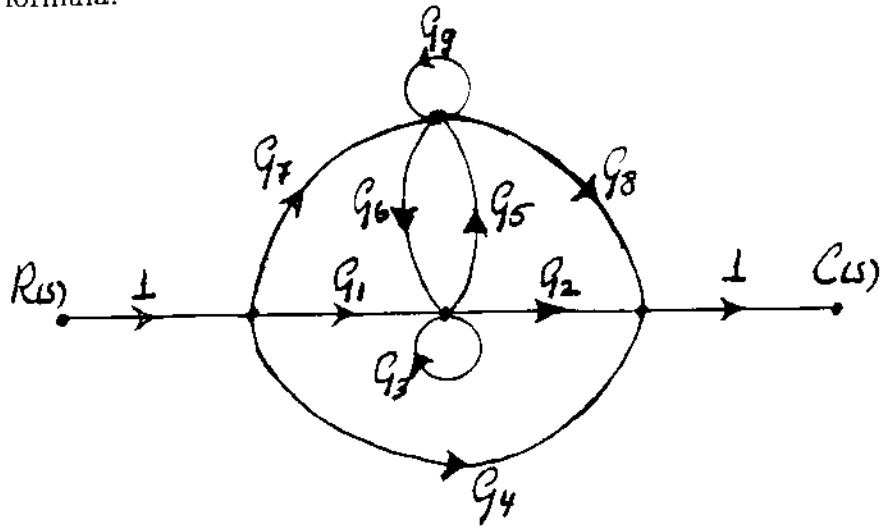
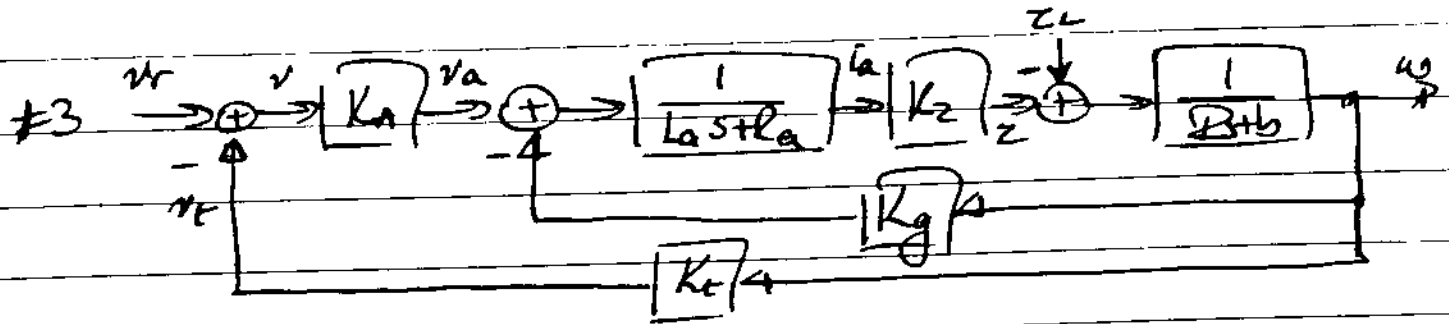
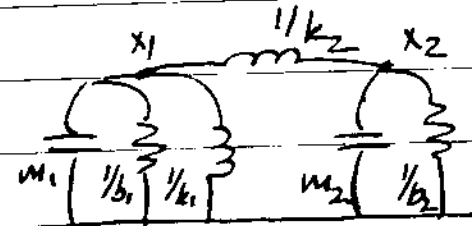
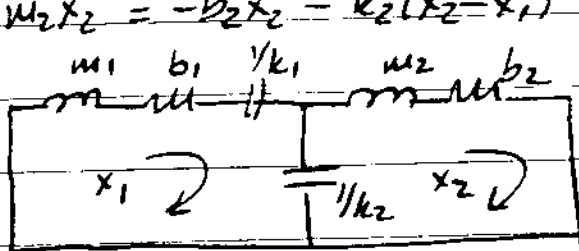


Figure 5:

#1  $F_1(s) = \frac{se^{-3Ts}}{(s+2)^2}$ ,  $f_1(t) = [1 - 2(t-3T)] e^{-2(t-3T)} u(t-3T)$   
 $F_2(s) = \frac{(s+1)e^{-3T(s+1)}}{(s+3)^2}$

#2  $m_1 \ddot{x}_1 = -b_1 \dot{x}_1 - k_1 x_1 - k_2(x_1 - x_2)$   
 $m_2 \ddot{x}_2 = -b_2 \dot{x}_2 - k_2(x_2 - x_1)$



#4  $\frac{Y(s)}{U(s)} = \frac{G_1(G_2 + G_3)}{1 - G_2G_4 + G_1(G_2 + G_3)G_4G_5}$

#5  $\frac{C(s)}{R(s)} = \frac{G_1G_2 - G_1G_2G_9 + G_7G_8 - G_3G_7G_8 + G_4 - G_3G_4 - G_4G_9 - G_9G_5G_6 + G_3G_4G_8 + G_1G_5G_8 + G_2G_6G_7}{1 - G_3 - G_9 - G_5G_6 + G_3G_9}$