

NAME _____

Math 12
Test 1
Spring 2011

You have 50 minutes to complete this test. You must *show all work* to receive full credit. Work any 8 of the following 9 problems. Clearly **CROSS OUT** the problem you do not wish me to grade. Each problem is worth 12 points, and you get 4 points for free, for a total of 100 points. The answers will be posted on the electronic reserves later today.

1. Use the *definition of the derivative* to find $f'(x)$ if $f(x) = \frac{1}{x^2}$.

2. Calculate the following limits.

(a) $\lim_{x \rightarrow 1} \left(\frac{1}{x^2} - \frac{1}{x} \right)$

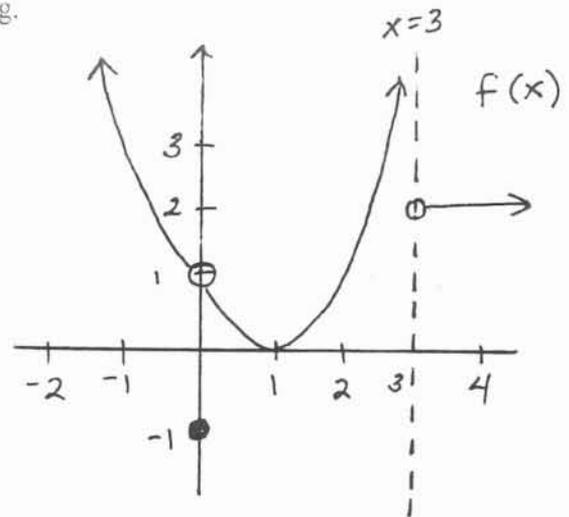
(b) $\lim_{x \rightarrow 1} \frac{x^2 + x - 2}{x^2 - 1}$

(c) $\lim_{x \rightarrow 1} \frac{\sqrt{x} - 1}{x - 1}$

3. A manufacturer can produce microwaves at a cost of \$80 apiece. If they are sold for x dollars each, $50 - x$ microwaves will be sold each month.
- Express the monthly profit as a function of the price x .
 - Sketch a graph of this profit function.
 - Estimate the price that will result in the highest profit.

4. Use the given graph to determine the following.

- $\lim_{x \rightarrow 4} f(x)$
- $\lim_{x \rightarrow 3^+} f(x)$
- $\lim_{x \rightarrow 3^-} f(x)$
- $\lim_{x \rightarrow 3} f(x)$
- $\lim_{x \rightarrow 0} f(x)$



- At what x -values is $f(x)$ discontinuous?

5. Find $f'(x)$ for the following functions. DO NOT simplify!

(a) $f(x) = \frac{2}{3x^2} - \frac{x}{3} + \frac{4}{5} + \frac{x+1}{x}$

(b) $f(x) = (x^2 + 2)(x + \sqrt{x})$

(c) $f(x) = \frac{x + 7x^{-4} + 3}{5 - 2x^2 + 3x}$

6. Find the equation of the line tangent to the graph of $f(x) = \frac{x + \sqrt{x}}{x\sqrt{x}}$ at the point where $x = 1$.

7. Find the equation of the line perpendicular to the line $x + 3y = 5$ which contains the point $(-2, 3)$.

8. Suppose x units of a product are produced and all units will be sold if the price is $p(x) = 25 - \frac{1}{3}x$ dollars per unit.

(a) Find the revenue function.

(b) Use the marginal revenue function to *estimate* the revenue derived from the sale of the 9th unit.

(c) Find the *actual* revenue derived from the sale of the 9th unit.

9. Sketch the graph of $f(x) = \begin{cases} x^2 & x < 2 \\ 9 & x \geq 2 \end{cases}$ and describe the continuity of this function.