

1.( pts.) (a) A complex number  $z$  is an ordered pair  $(x, y)$  of real numbers with addition and multiplication defined as:

(b) The complex number  $i$  is defined as the ordered pair:

(c) The modulus, complex conjugate, and polar form of the complex number  $z = (1,1) = 1 + i$  are, respectively:

(d) Euler's formula is  $e^{i\theta} =$

2.( pts.) (a) A subset  $S$  of the complex plane is called a domain if:

(b) Give an example of a set  $S$  of complex numbers which is a domain.

(c) Give an example of a set  $S$  of complex numbers which is not a domain and tell why.

(d) The Riemann sphere is:

(e) The stereographic projection maps \_\_\_\_\_ onto \_\_\_\_\_  
\_\_\_\_\_.

(f) A neighborhood of the point at infinity (denoted  $\infty$ ) is:

(g) The extended complex plane is:

3.( pts.) (a) We say that the complex number  $w_0$  is the limit of the function  $f = f(z)$  as  $z$  approaches  $z_0$  provided: