## **Projectile Notes**

- 1. Definition of a Projectile: An object that is "projected" or thrown, which has no capacity for self-propulsion.
- 2. Actual forces on a Projectile: Drag, lift due to spin, weight, wind.
- 3. Are the forces on a projectile (other than weight) significant?
  In other words, does the ideal projectile model "fit" or not?



For low speed objects with reasonable mass, e.g. a shot put, or a baseball, tennis ball or golf ball tossed softly across a room, the ideal projectile model "fits" relatively well.

For high speed objects, e.g. a hit or thrown baseball, a well-hit golf ball or tennis ball, etc., drag and other forces are significant and our ideal model is not accurate. For example, a well-hit home run, by ideal theory, will travel nearly 750 ft. In reality it only travels around 450 ft—a significant difference! Light objects, e.g. a ping pong ball, feather, foam ball, etc., do not fit the ideal model very well. A relatively small drag or spin force markedly affects the ball because the ball has such low mass.

**Interesting fact:** A well-hit golf ball travels farther than ideal theory predicts because of lift due to spin.



4. "Ideal" Projectile: The only force is weight. (This is what we will cover in this class.)

5. Ideal Projectile: If the only force is weight, then the x velocity stays constant. The y velocity changes with time and position.

6. Ideal Projectile: If the only force is weight, then...The x velocity stays constant.The y velocity changes with time and position.



7. Ideal Projectile Equations: If the only force is weight, then the x velocity stays constant  $(a_x = 0)$ . The y velocity changes with time and position (y acceleration  $a_y = -g$ ). Remember to use the correct g for your units!



## 8. An ideal projectile trajectory is a parabola.



We rarely use this fact to solve a problem, but you should know it. 9. For each launch speed,  $v_0$ , and angle  $\theta$  there is a different parabolic trajectory.



10. For a given launch speed,  $v_0$ , the max range is at  $\theta$  = 45. For the same  $v_0$ , launch angles at equal angular increments above and below 45 give (equal) ranges shorter than the max range.



For a given  $v_0$ , max range at  $\theta$  = 45° (on level ground)

For a given  $v_0$ , launch angles at equal angular increments above and below 45° give (equal) ranges shorter than the max range. 11. A general projectile motion problem involves seven "pieces" of information [ $x_0$ ,  $y_0$ ,  $\theta$ ,  $x_L$ ,  $y_L$ , and  $t_L$ ]. General Projectile Problem

V

Usually you are given five of these and asked to find the remaining two, usually applying the two position equations.



Projectile Problem Variables: (7 pieces of info) Launch Location:  $(x_0, y_0)$ Launch Velocity and Angle:  $(v_0 \text{ at } \theta)$ Landing Location and Time:  $(x_L, y_L)$  at time  $t_L$ 

General Problem: Given 5 out of 7 of these "pieces" of info.Use the two position equations to solve for the remaining two:Position:
$$x = x_0 + v_x t$$
 $y = y_0 + v_{0y}t - \frac{1}{2}gt^2$ where, $v_x = v_0 \cos \theta$  $v_{0y} = v_0 \sin \theta$