

Particle Straight Line (Graphical): Ex Prob 3

Given the $v(t)$ graph at right,
draw the $a(t)$ and $s(t)$ graphs.

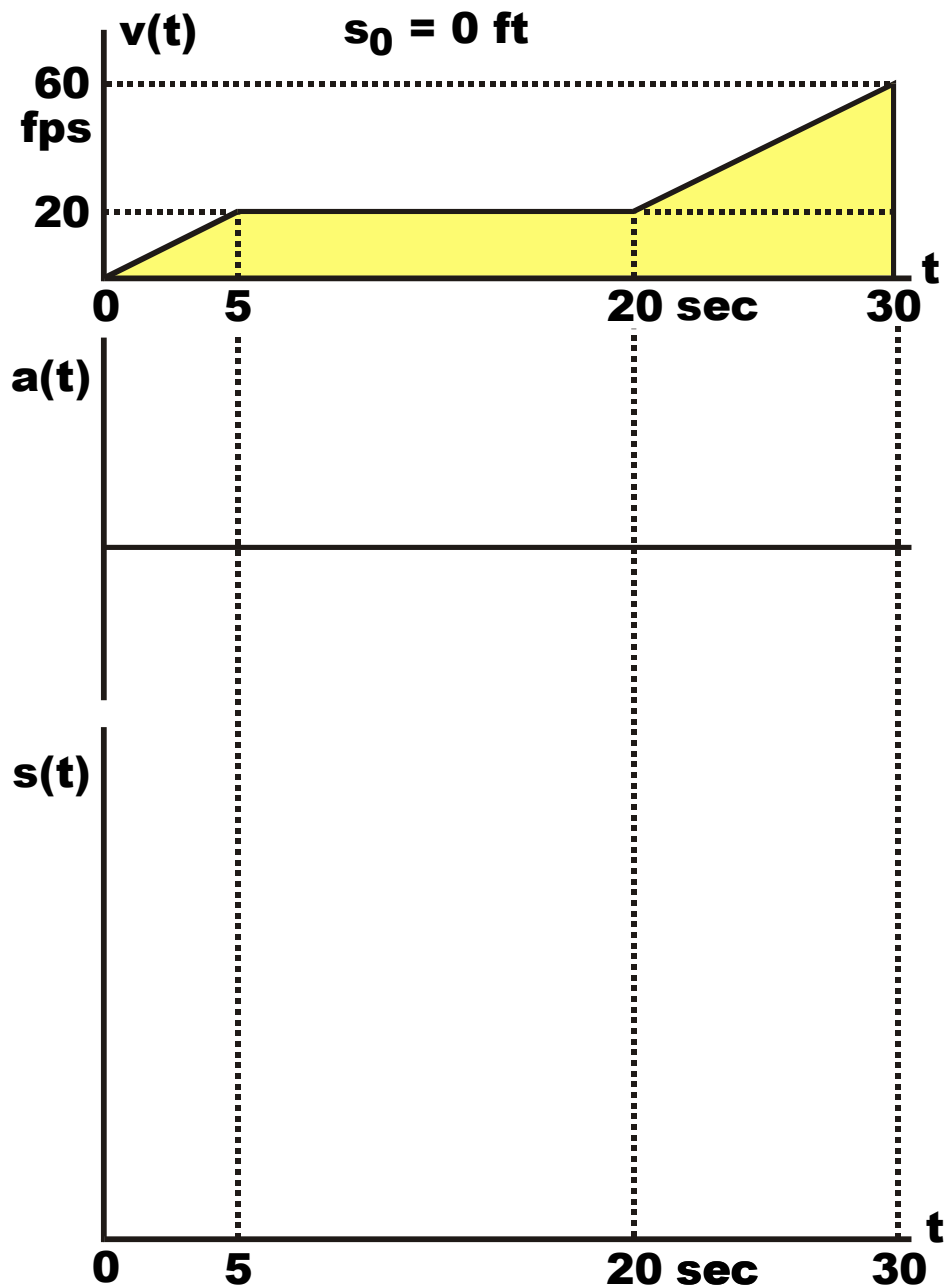
Defining Eqns

$$\textcircled{1} \quad a = \frac{dv}{dt}$$

$$\textcircled{2} \quad v = \frac{ds}{dt}$$

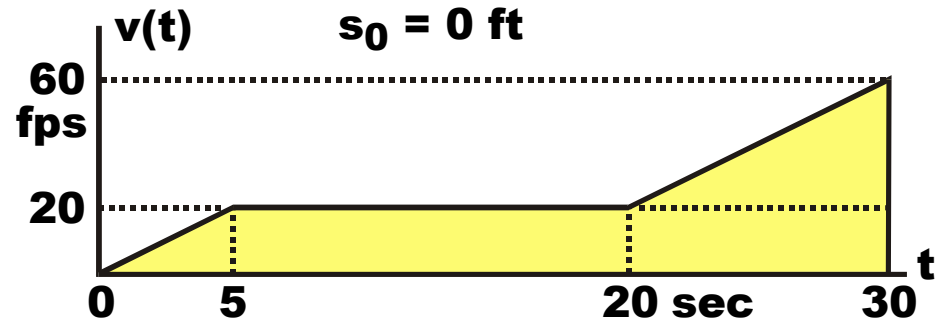
$$\textcircled{3} \quad a \, ds = v \, dv$$

To work this problem, you must
learn and be comfortable with
the graphical interpretation of
these defining equations.
(See the next page...)



A Graphical Problem

Understand the graphical interpretation of the defining kinematic equations!



Graphical Interpretation of the Defining Eqns

$$a = \frac{dv}{dt}$$

At a point, the acceleration
 a = slope of the $v(t)$ curve

$$\Delta v = \int a dt$$

Over an interval, the change in v
 Δv = area under the $a(t)$ curve

$$v = \frac{ds}{dt}$$

At a point, the velocity
 v = slope of the $s(t)$ curve

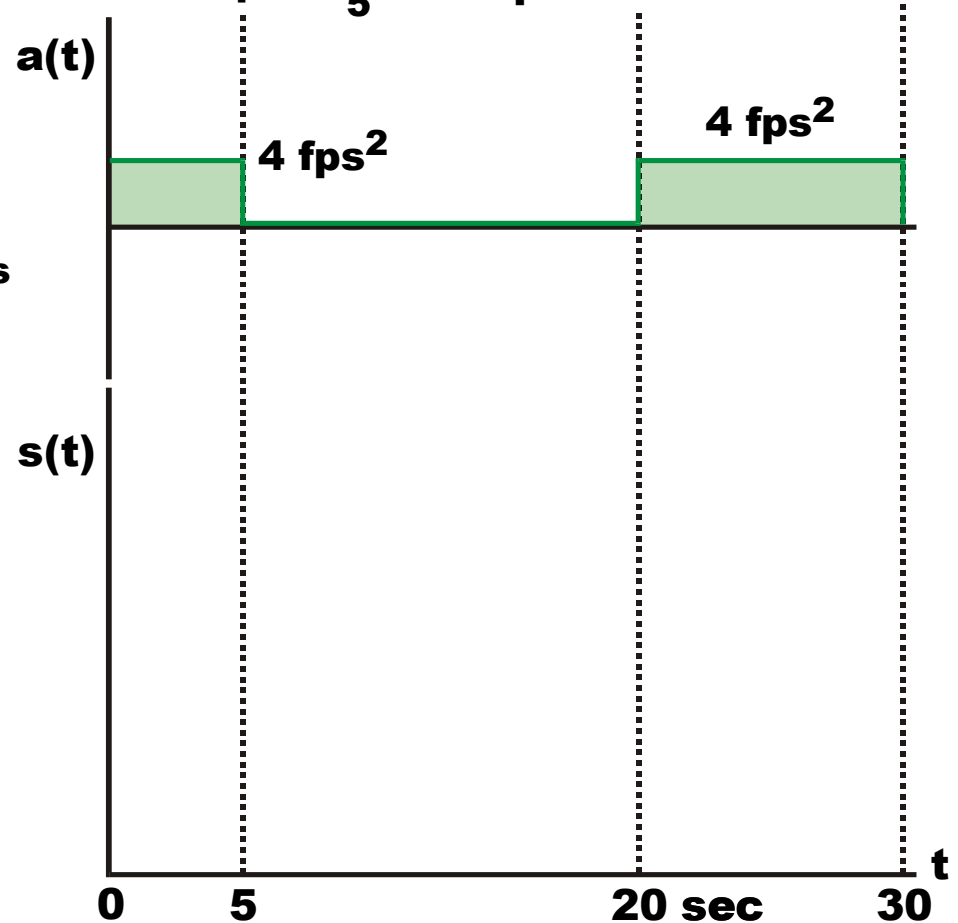
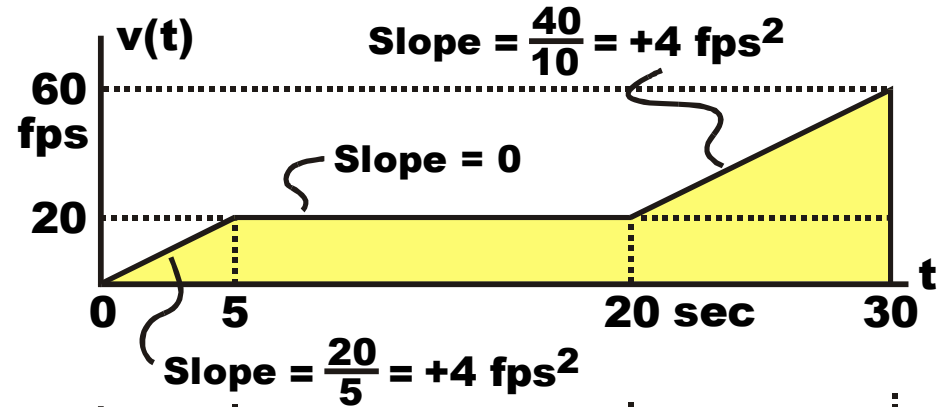
$$\Delta s = \int v dt$$

Over an interval, the change in s
 Δs = area under the $v(t)$ curve

A Graphical Problem

Given the $v(t)$ graph at right, draw the $a(t)$ and $s(t)$ graphs.

1. Accel = $v(t)$ slopes...



Graphical Interpretation of Defining Eqns

$$a = \frac{dv}{dt}$$

At a point,
 a = slope of $v(t)$ curve

$$\Delta v = \int a \, dt$$

Over an interval,
 Δv = area under $a(t)$ curve

$$v = \frac{ds}{dt}$$

At a point,
 v = slope of $s(t)$ curve

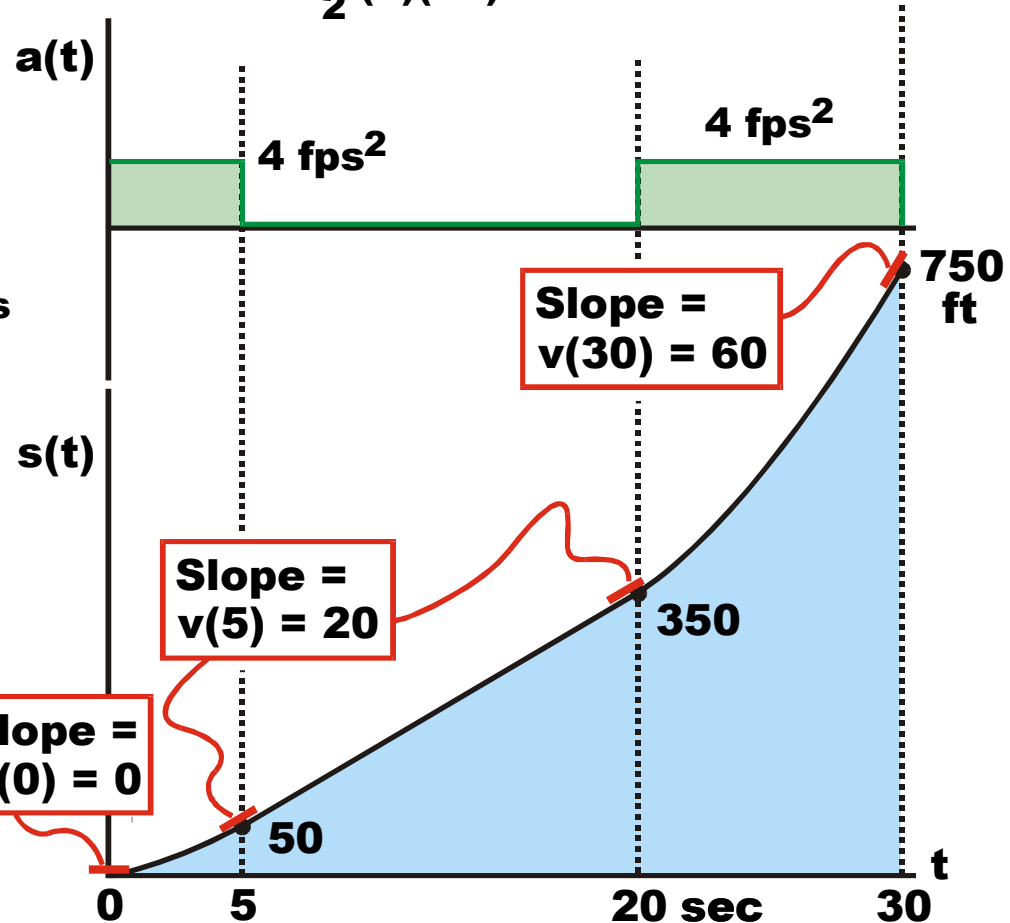
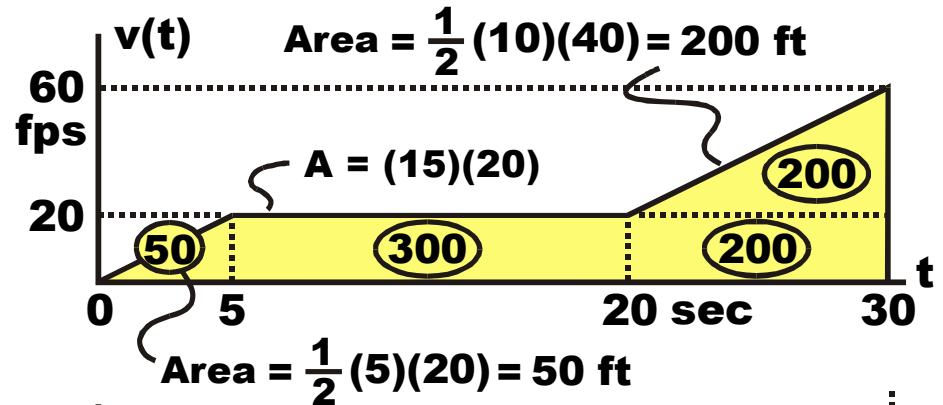
$$\Delta s = \int v \, dt$$

Over an interval,
 Δs = area under $v(t)$ curve

2. Find and label **areas**
under the **$v(t)$** curve...

These are Δs over the 0-5,
5-20, and 20-30 time intervals.

3. The $s(t)$ curve shapes
come from the slopes. At a
point, the **slope** of the $s(t)$
curve = **$v(t)$** at that point.



Graphical Interpretation of Defining Eqns

$$a = \frac{dv}{dt}$$

At a point,
 a = slope of $v(t)$ curve

$$\Delta v = \int a dt$$

Over an interval,
 Δv = area under $a(t)$ curve

$$v = \frac{ds}{dt}$$

At a point,
 v = slope of $s(t)$ curve

$$\Delta s = \int v dt$$

Over an interval,
 Δs = area under $v(t)$ curve