

Language Exploration



FUNDAMENTALS OF FUNCTIONAL PROGRAMMING.

1. No assignment. (Just labels)
2. Computation is performed by "function composition"
 - little or no sequential execution.
 - Recursion over iteration.
3. Functions are "first class" entities:
 - can be passed as arguments to functions
 - can be returned as return values of functions.

$$s(h(g(f(x))))$$

LISP

• History 1960 by John McCarthy

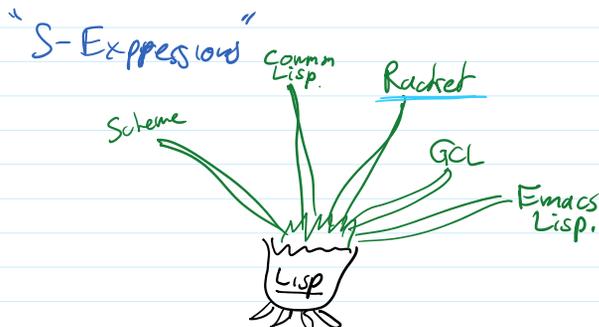


He was working on a "Model of computation" inspired by Alonzo Church's "lambda Calculus"

$f(x)$

$f.x$

$\lambda.x$ ← anonymous function that takes one parameter x



• The Core of Lisp:

Syntax

atom :- a sequence of letters or numbers or some symbols

e.g. foo apple 123 cat2 2cat
the_snake hello? a-b a+b

exceptions
; # ' ↑

expressions - an atom

or

- a list of zero or more expressions.

- separated by spaces
- enclosed in parenthesis.

e.g. foo (apple cat2) ()
(a b c) (apple)
(foo (bar) (apple 123))

Semantics: idea:

(a b c d) ↗ data.
↘ function apply function a to arguments b c d

• BASIC FORMS (pre-defined functions)

• (quote x) evaluates to x

e.g.

(quote a) → a

shorthand 'a → a

(quote (a b c)) → (a b c)

'(a b c) → (a b c)

• Special atoms

t - true

nil } false
() }

• (atom x) evaluates to t if x is an atom
nil otherwise.

e.g. $(\text{atom } \text{apple}) \Rightarrow \otimes$ apple is undefined
 $(\text{atom } ' \text{apple}) \Rightarrow t$
 $(\text{atom } '(a b c)) \Rightarrow \text{nil}$
 $(\text{atom } (a b c)) \Rightarrow \otimes$ a is undefined.
 $(\text{atom } (\text{atom } 'a)) \Rightarrow (\text{atom } 't) \Rightarrow t$
 $(\text{atom } \underbrace{(\text{atom } 'a)}_{\substack{\text{data} \\ \text{do not evaluate}}}) \Rightarrow \text{nil}$

- $(\text{eq } x y)$ evaluates to t if both x and y are atoms and are the same atom, or both the empty list. nil otherwise.

e.g. $(\text{eq } 'a 'a) \Rightarrow t$
 $(\text{eq } 'a 'b) \Rightarrow \text{nil}$
 $(\text{eq } 't (\text{atom } 'a)) \Rightarrow (\text{eq } 't 't) = t$

- $(\text{car } l)$ expects l to be a list and evaluates to the first element in list l

e.g. $(\text{car } '(a b c)) \Rightarrow a$
 $(\text{car } '(\text{apple banana})) \Rightarrow \text{apple}$
 $(\text{atom } (\text{car } '(a b c))) \Rightarrow (\text{atom } 'a) \Rightarrow t$

- $(\text{cdr } l)$ expects l to be a list and evaluates to the list after the first element of l

$(\text{cdr } '(a b c)) \Rightarrow (b c)$
 $(\text{cdr } '(a)) \Rightarrow ()$
 $(\text{cdr } (\text{cdr } '(a b c))) \Rightarrow (\text{cdr } '(b c)) \Rightarrow (c)$

- $(\text{cons } x y)$ expects y to be a list, and evaluates to the list that consists of x followed by y

$(\text{cons } 'a '(b c)) \Rightarrow (a b c)$
 $(\text{cons } '(b c) '(d e)) \Rightarrow ((b c) d e)$

• Conditional Form:

$(\text{cond } (p_1 e_1) (p_2 e_2) (p_3 e_3) \dots (p_n e_n))$

• the p expressions are evaluated in order until one evaluates to t , then the corresponding e expression is evaluated, and its result is the value of the whole cond expression.

• evaluates to nil if no p expression evaluates to t .

e.g. $(\text{cond } (\overbrace{(\text{eq } 'a 'b)}^p) \overbrace{'first'}^e) (\text{atom } 'a) 'second (\text{atom } 'b) 'third) \Rightarrow \text{second}$

• Functional Forms

• $(\text{lambda } (p_1 p_2 \dots p_n) e)$

an anonymous function with parameters $p_1 \dots p_n$ and expression e as its body

e.g. $(\text{lambda } (a b c) (\text{cons } a (\text{cons } b (\text{cons } c \text{ nil}))))$

• $(\text{funcall } f (p_1 p_2 \dots p_n))$ expects f to be a function evaluates to f applied to arguments $p_1 \dots p_n$

e.g. $(\text{funcall } (\text{lambda } (a b c) (\text{cons } a (\text{cons } b (\text{cons } c \text{ nil})))) ('apple 'banana 'orange)) \Rightarrow (\text{apple } \text{banana } \text{orange})$

• $(\text{defun } \text{foo } (p_1 p_2 \dots p_n) e)$ defines a named function foo with parameters $p_1 \dots p_n$ and body e .

e.g. $(\text{defun } \text{make-triple } (a b c) (\text{cons } a (\text{cons } b (\text{cons } c \text{ nil}))))$

(make-triple 'apple 'orange 'banana) ⇒ (apple orange banana)

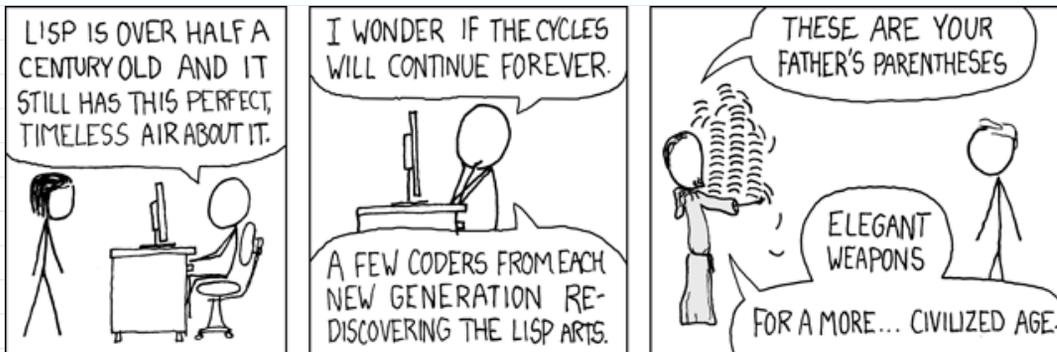
more example functions

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(defun is-null? (x)
  (eq x nil))
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```
(defun and (x y)
  (cond (x (cond (y t)
                 (t nil)))
        (t nil) ))
```

```
(defun append (l x)
  (cond (eq l '()) (cons x '())
        (t (cons (car l)
                  (append (cdr l) x))))))
```

$[h \cdot \overset{l}{\dots}] \times \Rightarrow [h \dots x]$
 $h = \overset{cons.}{[\dots x]}$



Demo !!