Lithospheric Structure and Evolution of Southern Africa: Constraints from Joint Inversion of Rayleigh Wave Dispersion and Receiver Functions

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Key Points:

• A 3-D shear wave velocity model is obtained for southern Africa from joint inversion of Rayleigh wave dispersion and receiver functions
• The Okavango dyke swarm and Bushveld intrusion led to crustal underplating and reduced mantle velocities due to lithospheric refertilization
• Thicker crust, lower elevation, and higher crustal Vs in the Limpopo belt relative to the Kaapvaal craton indicate lower crustal eclogitization

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Abstract

We conduct the first joint inversion of teleseismic receiver functions and Rayleigh wave phase velocity dispersions from both ambient noise and earthquakes using data from 79 seismic stations in southern Africa, which is home to some of the world’s oldest cratons and orogenic belts. The area has experienced two of the largest igneous activities in the world (the Okavango dyke swarm and Bushveld mafic intrusion), and thus is an ideal locale for investigating continental formation and evolution. The resulting 3-D shear wave velocities for the depth range of 0-100 km and crustal thickness measurements show a clear spatial correspondence with known geological features observed on the surface. Higher than normal mantle velocities found beneath the southern part of the Kaapvaal craton are consistent with the basalt removal model for the formation of cratonic lithosphere. In contrast, the Bushveld complex situated within the northern part of the craton is characterized by a thicker crust and higher crustal $V_p/V_s$ but lower mantle velocities, which are indicative of crustal underplating of mafic materials and lithospheric refer-tilization by the world’s largest layered mafic igneous intrusion. The thickened crust and relatively low elevation observed in the Limpopo belt, which is a late Archean collisional zone between the Kaapvaal and Zimbabwe cratons, can be explained by eclogitization of the basaltic lower crust. The study also finds evidence for the presence of a stalled segment of oceanic lithosphere beneath the southern margin of the Proterozoic Namaqua-Natal mobile belt.

1 Introduction

Southern Africa comprises the Archean Zimbabwe and Kaapvaal cratons and several mobile belts formed between 2.7 and 0.3 Ga (Figure 1). Assembled before 3.0 Ga, the crust of the Kaapvaal craton is as old as 3.7 Ga in the eastern-southeastern parts of the craton (Compston & Kroner, 1988; Hamilton et al., 1979; Kroner et al., 1996; Thomas et al., 1993). Separated by a NNE trending strike-slip/thrust belt from the oldest core of the craton, the Neo-Archean (3.0 - 2.5 Ga) crust is exposed on the western side of the craton. The north-central portion of the Kaapvaal craton is occupied by the Bushveld complex, which has an estimated age of intrusion of 2.05 Ga (de Wit et al., 1992) and is the largest known layered mafic intrusion in the world (Buick et al., 2001; Von Gruenewaldt et al., 1985; Walraven & Hattingh, 1993). The Zimbabwe craton consists of Archean rocks that formed between 3.6 and 2.5 Ga (Jelsma & Dirks, 2002; Wilson, 1990).
craton was stabilized after an enigmatic regional-scale melting in the crust at about 2.57 Ga, probably due to a delamination event (Hickman, 1978; Treloar & Blenkinsop, 1995). Formed by the collision between the Zimbabwe craton to the north and the Kaapvaal craton to the south at around 2.7 Ga, the Limpopo orogenic belt lies in an east-west trending band and separates the two cratons. Composed of Proterozoic metamorphosed rocks ranging from ~2.0 to ~1.0 Ga, the Namaqua-Natal mobile belt was amalgamated to the Kaapvaal craton during the Namaqua Orogeny between 1.3 to 1.0 Ga, and the youngest tectonic province of the study area, the Cape foldbelt (0.3 Ga) located at the southern end of Africa, was formed during the late-Proterozoic/early-Cambrian Saldanian Orogeny and the late-Paleozoic Cape Orogeny (Rozendaal et al., 1999).

A number of seismological investigations have been conducted in southern Africa to characterize the thickness, composition, and tectonic evolution of the crust and uppermost mantle. Nair et al. (2006) use receiver functions (RFs) to estimate crustal thickness ($H$) and $V_p/V_s$ ($\kappa$) using data from the Southern African Seismic Experiment (SASE). A thicker than normal crust is observed in the western Zimbabwe craton, the Limpopo belt, the Bushveld complex, and the Namaqua-Natal mobile belt. The study also reveals a 12 km thickness intruded mafic layer at the bottom of the crust beneath the Bushveld complex. While most other $H - \kappa$ studies (e.g., Delph & Porter, 2015; Youssof et al., 2013) generally agree with the crustal thickness results of Nair et al. (2006), the resulting $\kappa$ measurements are more diverse. Youssof et al. (2013) argue a paleocollisional zone rather than a mafic layer intrusion beneath the central part of the Bushveld complex on the basis of the overall felsic composition which is indicated by a low $V_p/V_s$ of 1.68 - 1.70, a range that is significantly different from most previous RF studies (e.g., Nair et al., 2006).

Ravenna et al. (2018) perform a surface (Rayleigh and Love) wave phase velocity probabilistic Bayesian inversion to construct shear wave velocity structure beneath the Kaapvaal craton and the Limpopo belt, from the upper crust to the upper mantle. The inverted shear wave velocity curves indicate a thinned lithosphere beneath the central-southwestern Kaapvaal craton and a slightly-to-moderately depleted lowermost lithosphere beneath the Limpopo orogenic belt. Yang et al. (2008) obtain shear wave velocities in southern Africa from the surface to 100 km depth using surface wave ambient noise to-mography (ANT) for short periods and two-plane-wave method for longer periods. Their results show that velocities in the uppermost crust are well correlated with the geolog-
critical units, and high velocities beneath the cratonic regions are mainly due to the existence of more mafic Archean crust. In the uppermost mantle, relatively high velocities are observed under the thinner Archean crust, and low velocities are found beneath the thicker Proterozoic crust (Yang et al., 2008). Using a two-plane-wave tomography technique, Li (2011) and Li & Burke (2006) investigate the approximately same area from surface to 410 and 310 km depths, respectively. Both studies observe that the Bushveld complex is relatively slower than its surrounding areas, suggesting a high iron content from an intracratonic intrusion at 2.05 Ga. Li & Burke (2006) also propose that a low velocity zone at the depth range of 160 to 260 km across southern Africa is mainly caused by high temperature, which probably supports the high elevation of southern Africa. In contrast, Adams & Nyblade (2011) map shear wave velocities from 50 to 350 km by inverting surface wave phase velocities. Their velocity model is not consistent with the existence of a positive temperature anomaly beneath southern Africa.

Comparing with surface wave tomography, RFs possess the ability to improve the vertical resolution and could better image internal interfaces (Deng et al., 2015; Shen et al., 2013; Shen & Ritzwoller, 2016). However, RFs only provide information near seismic stations and have lower resolution for structures between discontinuities than surface wave tomography (e.g., Ammon et al., 1990). Although southern Africa has been investigated by numerous studies, this study provides a high-resolution 3-D shear wave velocity model from a joint inversion of surface wave dispersion and RFs. To our knowledge, this is the first study to obtain surface wave phase velocity dispersion from both ambient seismic noise (for shorter periods) and teleseismic earthquakes (for longer periods) data. Rayleigh wave phase velocity maps at different periods are obtained by inverting phase velocity dispersion measurements derived from ambient seismic noise at short periods (6 - 24 s) and teleseismic earthquakes at long periods (28 - 80 s). Additionally, a non-linear Bayesian Monte-Carlo approach is applied to obtain 3-D shear wave velocity model beneath southern Africa.

2 Data and Methods

2.1 Data

The data used in the study were recorded by 79 SASE seismic stations between April, 1997 and December, 1999 located in the area of 16°E - 34°E, and 36°S - 18°S (Figure
1). The data set is archived at the Incorporated Research Institutions for Seismology (IRIS) Data Management Center (DMC) and is publicly accessible. For the ambient noise tomography study, we requested continuous broadband vertical-component waveforms, each with a length of 86400 s (1 day), from the IRIS DMC. The seismograms were resampled to 5 samples per second, and Rayleigh wave phase velocity dispersion measurements from 6 to 30 s with an interval of 2 s were then calculated from the empirical Green’s function (EGF) analysis (Yao et al., 2006, 2008, and 2010). For the two-station earthquake Rayleigh wave phase velocity dispersion measurements (Yao et al., 2005), broadband seismic data with a sampling frequency of 1 Hz were requested from a total of 384 $M_b \geq 5.7$ earthquakes in the epicentral distance range of $10^\circ$ - $130^\circ$. The period range is from 20 to 80 s with an interval of 4 s.

To compute RFs, data from teleseismic events in the epicentral distance range of $30^\circ$ to $100^\circ$ were requested from the DMC. The cutoff magnitude ($M_c$) used for selecting earthquakes is calculated by $M_c = 5.2 + (\Delta - 30.0)/(180.0 - 30.0) - D/700.0$, where $\Delta$ and $D$ are the epicentral distance in degree and focal depth in kilometer, respectively (Liu & Gao, 2010). A total of 5653 three-component seismograms from 166 teleseismic events that satisfy the above epicentral distance range and $M_c$ criterion were chosen for the period of 4/10/1997 - 12/31/1999. The seismograms were windowed 20 s before and 30 s after the first theoretical P-wave arrival based on the IASP91 Earth model (Kennett & Engdahl, 1991).

2.2 Methods

2.2.1 Rayleigh wave Data Processing for ANT

The procedure of data processing used here is generally the same as that in Wang et al. (2019), and is briefly described below. The procedure includes the following steps: (1) single-station preprocessing, (2) cross-correlations and temporal stacking, (3) phase velocity dispersion measurements, and (4) inversion for phase velocities. Details about the steps can be found in previous studies (e.g., Bensen et al., 2007; Sabra et al., 2005; Shapiro et al., 2005; Shapiro & Campillo, 2004; Weaver, 2005; Weaver & Lobkis, 2004).

In the single-station preprocessing step, the mean, linear trend, and the instrumental response are firstly removed, and a second-order Butterworth filter in the frequency range of 0.025 - 0.5 Hz is utilized, followed by temporal normalization to reduce the in-
terference from earthquakes, instrumental irregularities, and non-stationary noise. Spectral whitening is then applied to produce broadband ambient noise signals.

The next step is to compute cross-correlations and perform temporal stacking. The total number of possible daily cross-correlation series is 3081 ($N = n(n-1)/2$, where $n$ is the number of stations). Because not all the 79 stations were operating in a common period, a total of 2245 possible inter-station cross-correlation series were produced. All the daily cross-correlation series for each station pairs are then stacked, and the causal and acausal signals are symmetrically averaged to enhance the signal-to-noise ratio (SNR). A negative time derivative of the stacked cross-correlation series is taken to estimate Rayleigh wave EGFs from the stacked cross-correlation series. Figure 2 shows the raypaths and cross-correlation series between Station SA38 and all the other stations.

Subsequently, phase velocity dispersion curves are estimated from the EGFs based on a modified far-field approximation and an image transformation analysis (Yao et al., 2005, 2006, and 2010). Three criteria are imposed to reject unreliable dispersion measurements: (1) the distance between two stations should be at least three times of the longest wavelength, (2) the SNR for each of the stacked cross-correlation series should be equal or larger than 5.0, and (3) the phase velocity dispersion curves should be similar to the global model of Shapiro & Ritzwoller (2002).

The final step involves inverting for Rayleigh wave phase velocities using the phase velocity dispersion measurements obtained from the previous step (Tarantola & Nercessian, 1984; Tarantola & Valette, 1982). The phase velocities are for periods between 6 and 30 s with an interval of 2 s, and the horizontal grid dimension is $0.4^\circ \times 0.4^\circ$ with a sampling step of 0.1$^\circ$.

### 2.2.2 Rayleigh Wave Data Processing for Earthquake Tomography

The two-station method is utilized to determine fundamental mode Rayleigh wave phase velocities in the period range of 20 - 80 s (Yao et al., 2005). Based on an image analysis technique (Yao et al., 2004), a MATLAB GUI software is applied to implement the determination of the phase velocity dispersion curves (Yao et al., 2005). The two-station analysis is under the assumption that surface-wave propagation is along a great-circle path between the earthquake and station. First, the instrumental responses of station records with clear Rayleigh wave trains are removed. Subsequently, the multiple fil-
The technique (Dziewonski et al., 1969) is applied to determine group arrival times of Rayleigh wave fundamental mode, and to obtain the cross-correlation amplitude image for each of the station pairs. Third, a 3-spline interpolation is applied to transform the cross-correlation amplitude image into a phase velocity image for directly judging the quality of phase velocity dispersion curves (Yao et al., 2006). The selected phase velocity dispersion measurements are inverted using the same technique as that applied in the EGF analysis. Phase velocity maps are constructed for periods between 20 and 80 s with an interval of 4 s. The grid dimension and sampling step are the same as those for the ANT analysis. The study area was divided into $0.2^\circ \times 0.2^\circ$ grids, and those with at least one ray path were retained.

### 2.2.3 Receiver Function Data Processing

A four-pole, two-pass band-pass Bessel filter with a frequency range of 0.06 - 1.2 Hz is applied to the original seismograms to enhance the signals, and to reject events with SNR of less than 4.0. The SNR is calculated using $\text{SNR} = \max|A_s|/|\bar{A}_n|$, where $\max|A_s|$ represents the maximum absolute amplitude on the vertical seismograms in the time window of 8 s before and 17 s after the predicted IASP91 arrival time for the first P-wave, and $|\bar{A}_n|$ represents the mean absolute amplitude in the time window of 10 - 20 s before the predicted P-wave arrival time (Gao & Liu, 2014). We next apply a frequency-domain water-level deconvolution procedure (Ammon et al., 1990) to convert the filtered seismograms into radial receiver functions.

The $H - \kappa$ RF stacking procedure (Zhu & Kanamori, 2000) is applied to search for the optimal $H$ and $\kappa$ pair. The weighting factors used in the study are 0.5, 0.3, and 0.2 for the $PmS$, $PPmS$, and $PSmS$ phases, respectively, which are the same as those in Nair et al. (2006). The bootstrap resampling approach (Efron & Tibshirani, 1986; Press et al., 1992) with 10 iterations is utilized to compute the mean values of $H$ and $\kappa$ and to estimate their standard deviations. Figure 3 shows an example of the $H - \kappa$ diagrams.

### 2.2.4 Joint Inversion of Surface Wave Dispersion and Receiver Functions

Surface wave dispersion measurements are sensitive to absolute shear wave velocities and can be used to constrain the vertically averaged velocity profile (Deng et al.,
In comparison, RFs can provide reliable constraints on vertical velocity contrasts, such as the Moho discontinuity and bottom of the sedimentary layer, which are difficult to resolve using surface wave dispersion alone. Consequently, RFs can effectively complement surface wave dispersion (e.g., Bodin et al., 2012; Julia et al., 2000; Ozalaybey et al., 1997), and the results from joint inversion of surface wave dispersion and receiver functions are more reliable than those obtained on either data set alone (e.g., Julia et al., 2005; Shen et al., 2013). In this study, we apply a non-linear Bayesian Monte-Carlo technique (Shen et al., 2013) to construct a 3-D shear wave velocity structure, from the surface to the depth of 100 km, by jointly inverting Rayleigh wave phase velocity dispersion and RFs.

Similar to Shen et al. (2016), three prior constraints are employed during the process of the Monte-Carlo sampling: (1) shear wave velocity gradually increases with depth through the discontinuity at the Moho, (2) shear wave velocity monotonically increases with depth through the entire crystalline crust, and (3) shear wave velocity is no more than 4.9 km/s for all depths. Considering the values of $H$ and $\kappa$ vary from station to station, we generate one initial model for each of the stations. For stations with reliable RF measurements, Rayleigh wave phase velocities and RFs are jointly inverted. For stations without reliable RF measurements (SA04, SA20, SA49, SA51, SA57, and SA67), only the surface wave phase velocities are inverted. Two principal layers are stratified into the initial models for the inversion. The top layer is the crystalline crust, which has a layer thickness $H$ obtained from the $H-\kappa$ stacking of RFs, and the shear wave velocity is obtained using a 4 cubic B-spline interpolation. The bottom layer has a depth range of $H-100$ km and the interpolation is performed using 5 cubic B-spline interpolation. Scaling relations (Christensen & Mooney, 1995; Karato, 1993) are applied to estimate the densities in the crust and upper mantle. The Q values in the PREM model (Dziewonski & Anderson, 1981) are utilized to conduct physical dispersion corrections by applying the approach of Kanamori & Anderson (1977). In the crust, the $\kappa$ values for the initial models are derived from the RFs, while in the upper mantle it is fixed at 1.75. Figure 4 shows initial models for stations located in different regions.
3 Results

3.1 Rayleigh Wave Phase Velocity Tomography

3.1.1 Phase Velocity Maps from ANT

By inverting a total of 515 reliable phase velocity dispersion measurements, 2-D phase velocity maps for the periods of 6 to 30 s are obtained with 0.4° × 0.4° spatial grids. Figures 5a, 5b, and 5c show phase velocity maps at the periods of 6, 16, and 24 s, respectively. The resulting spatial distribution of phase velocities correspond well with known geological features. At the period of 6 s (Figure 5a), low phase velocity anomalies are observed in the northern and eastern Kaapvaal craton, eastern part of the boundary between the Zimbabwe craton and the Limpopo belt, the Namaqua-Natal mobile belt, and the Cape foldbelt. The low phase velocity anomalies are mainly attributed to relatively thick sedimentary layers (de Wit et al., 1992; de Wit & Tinker, 2004; Durrheim & Green, 1992; Green & Durrheim, 1990). Relatively high phase velocities are observed in most parts of the Zimbabwe craton and the Limpopo belt, and the central and western Kaapvaal craton, and are most likely due to the existence of a more mafic Archean upper crust (Durrheim & Mooney, 1994). Low phase velocity anomalies observed at the period of 6 s persist at the period of 16 s in most areas (Figure 5b). For the period of 24 s (Figure 5c), the high phase velocities beneath the central Zimbabwe craton expand to the entire cratonic area and become more evident. Most of the southern Kaapvaal craton is characterized by relatively high phase velocities.

3.1.2 Phase Velocity Maps From Earthquake Tomography

Phase velocity maps at the period of 24 s from both the EGF and two-station analyses (Figures 5c and 5e, respectively) are plotted for comparison, and Figure 5d shows the differences. The patterns of the distribution of the phase velocities are similar with each other, and differences with an absolute amplitude greater than 0.05 km/s are observed only in a few locations (Figure 5d). Considering that the EGF analysis can provide more reliable phase velocity measurements at shorter periods (Yao et al., 2006), we use phase velocity measurements from the EGF analysis for the periods of 6 to 24 s, and those from the two-station analysis for the periods of 28 to 80 s. Figure 6 shows averaged Rayleigh wave phase velocity curves derived from both the EGF and two-station techniques.
At the periods of 32 and 40 s (Figures 5f and 5g), relative to the southern Kaapvaal craton, slow velocities are revealed for the central part of the Bushveld complex, the northern Namaqua-Natal mobile belt, and the Cape foldbelt. At the period of 60 s (Figure 5h), low velocities appear in the northeastern portion of the Zimbabwe craton and the northern Limpopo belt, the southwestern part of the Kaapvaal craton, and Bushveld and Venterdrop complex. At the period of 80 s (Figure 5i), the velocities within the southern Kaapvaal craton become comparable with the rest of the study area, except for the Cape foldbelt which continues to show low velocities.

3.2 Resolution Test

We conduct standard synthetic checkerboard test to investigate the resolution of the resulting phase velocities at different periods (Figure 7). For each of the periods, the input velocity model is composed of alternating positive and negative velocity anomalies with a 5% magnitude relative to 4 km/s in $2.0^\circ \times 2.0^\circ$ blocks (Figure 7a).

The events and stations used to generate the synthetic data are exactly the same as those in the real data, and the same inversion method was applied to obtain the recovery data. Figures 7b-7h show the recovered velocity models for the periods of 6, 16, 24, 32, 40, 60, and 80 s with the same ray-path coverage. The pattern of the checkerboard and the magnitude of anomalies can be well reconstructed for all the periods. Even though lateral smearing is more observable at longer periods (e.g., 60 and 80 s), the velocity anomalies are still resolvable in most of the study area. In general, the checkerboard test suggests that the resulting phase velocities are acceptable for all the periods.

3.3 Crustal Thickness From Receiver Functions

A total of 1976 high-quality RFs from 164 teleseismic events recorded by 73 out of the 79 seismic stations were used to obtain $H$ and $\kappa$ measurements. The resulting $\kappa$ values range from 1.68 at Station SA47 located within the Bushveld complex to 1.88 at Station SA03 in the Cape foldbelt, with an average value of $1.75\pm0.04$. Most stations within or adjacent to the Bushveld complex exhibit higher $\kappa$ values than the rest of the study area. The resulting $H$ values range from 28.1 km at Station SA01 in the Cape foldbelt to 53.3 km at Station SA47 in the Bushveld complex, with a mean value of $40.3\pm4.0$ km. Relatively thin crust is observed in the Cape foldbelt, central and southern Kaap-
vaal craton, and northern Zimbabwe craton. The crust thickens within the Namaqua-
Natal mobile belt, the Bushveld complex, the Limpopo belt, and the southwestern Zim-
babwe craton.

3.4 Joint Inversion Results

To more realistically reveal the velocity distribution at a given depth, we jointly
inverted Rayleigh wave phase velocity dispersion and RF measurements to obtain shear
wave velocities beneath each of the stations. Figure 8 shows the input data and results
for the joint inversion for two of the stations.

3.4.1 Shear Wave Velocity Structures

At the depth of 6 km, low shear wave velocity anomalies are mainly observed be-
neath the northern and eastern parts of the Kaapvaal craton, the Namaqua-Natal mo-
 bile belt, and the Cape foldbelt in the uppermost crust (Figures 9a and 10) and are mostly
related to the presence of a thick sedimentary cover. At the depth of 20 km (Figures 9b),
Cape foldbelt continues to demonstrate low velocities, and the Namaqua-Natal mobile
belt shows higher velocities relative to the Kaapvaal craton.

Velocity variations in the depths of 30 and 40 km (Figures 9c and 9d) are mainly
affected by the depth variation of the Moho discontinuity, where sudden increase in ve-
locity appears in areas with a crust that is shallower than the depth of the slice. At the
depth of 30 km (Figure 9c), velocities as fast as \(\sim\)4.15 km/s are observed beneath the
southern tip of the Cape foldbelt, suggesting that the crust in this area is thinner than
30 km. Similarly, beneath the central and southern Kaapvaal craton and northeastern
Zimbabwe craton, the high velocities observed in Figure 9d indicate that the crust is thin-
ner than 40 km. Relative to the adjacent mobile belts, the Kaapvaal and Zimbabwe cra-
tons show higher velocities from 50-100 km, while the Cape foldbelt is characterized by
relatively low velocities in the same depth range. A zone of high velocities along the south-
ern margin of the Namaqua-Natal mobile belt persists in the depth range of 50-100 km.
The sheet-like shape of the high velocity feature can be more clearly observed along the
cross-section shown in Figure 10.
3.4.2 Crust Thickness Distribution

Based on the assumption that the Moho is a sharp gradient interface across which the shear wave velocity experiences the most rapid increase, we obtained the $H$ measurements beneath the seismic stations by searching for the largest velocity gradient within the depth range of 20 to 60 km from the inverted 1-D shear wave velocity curve for each of the stations.

The resulting $H$ values from the joint inversion (Figure 11a) range from 28.5 km at Station SA01 at the southern tip of the Cape foldbelt to 52.0 km at Station SA70 located at the southwest corner of the Zimbabwe craton, with a mean value of 39.5 ± 4.0 km over the entire study area. For most of the stations, the crustal thickness difference obtained using the joint inversion (Figure 11a) and $H−κ$ stacking (Figure 11b) is less than 3 km (Figure 11c), and are in general agreement with previous crustal thickness studies (Delph & Porter, 2015; Kgawane et al., 2009; Nair et al., 2006; Yang et al., 2008; Youssof et al., 2013). Both the Kaapvaal and Zimbabwe cratons are characterized by a crustal thickness of about 36 km, which is typical for cratons. Thicker than normal crust is found in the Bushveld complex, the Limpopo belt, and southwestern Zimbabwe craton, and the Namaqua-Natal mobile belt, while the Cape foldbelt has the thinnest crust of less than 30 km.

4 Discussion

4.1 Basalt Removal in the Kaapvaal Craton

The Kaapvaal craton, with the exception of the Bushveld complex, is characterized by shear wave velocities of about 4.6 km/s, which is about 3% higher than the ~4.47 km/s value in most global models such as AK135 (e.g., Kennett et al., 1995). This increase in seismic velocities and the corresponding decrease in the density of the mantle lithosphere (See Figure 12 in Artemieva & Vinnik, 2016) are consistent with the basalt removal model for the formation of continental tectosphere (Jordan, 1975; 1988).

4.2 Lithospheric Modification in the Southwestern Zimbabwe Craton by the Okavango Dyke Swarm

The resulting $H$ measurements for the Zimbabwe craton (Figure 11a) demonstrate a large difference between the northeastern (NE) and southwestern (SW) portions of the
craton. The former has a relatively thin crust with a mean value of 36.8±1.3 km, and the latter has a thicker crust of 44.8±5.1 km. In addition, on the depth slides of 50-60 km (Figures 9e and 9f), the mean shear wave velocities beneath the SW Zimbabwe craton is about 0.9% lower than that beneath the NE part of the craton. The SW portion of the craton also shows a higher lithospheric density than the NE part (Artemieva & Vinnik, 2016).

One of the possible causes of the thickened crust, reduced upper mantle velocities, and the increased mantle density beneath the SW Zimbabwe craton is the emplacement of the mafic Okavango dyke swarm at about 179 Ma (Delph & Porter, 2015; Le Gall et al., 2005; Reeves, 2000; Youssof et al., 2013). The observed crustal thickening can be reasonably attributed to massive magmatic intrusion into the crust and magmatic underplating beneath the original Moho associated with the dyke swarm event. The intrusion of the mafic dykes into the subcrustal lithosphere could also result in lithospheric refertilization, leading to the observed reduction in seismic velocities (Figures 9e and 9f) and increase in mantle density (Artemieva & Vinnik, 2016; Jordan, 1979). The observed amplitude of velocity decrease (about 0.9%) in the upper-most mantle lithosphere beneath the SW Zimbabwe craton is consistent with the estimated velocity decrease due to lithospheric refertilization (Jordan, 1979). Finally, the increase in the density of the subcrustal lithosphere due to the refertilization compensates the mass deficit associated with the thickened crust, resulting in the near zero isostatic gravity anomaly in the area (Gwavava et al., 1996).

### 4.3 Magmatic Underplating and Lithospheric Refertilization Beneath the Bushveld Complex

Relative to the surrounding cratonic area, the crust beneath the Bushveld complex has a thickness that is about 5 km greater (Figure 11a). Similar to the SW Zimbabwe craton, the shear wave velocity in the subcrustal lithosphere beneath the Bushveld complex is lower than that in the southern Kaapvaal craton (Figure 12), and the lithospheric density is higher (Artemieva & Vinnik, 2016). Additionally, the crustal \( V_p/V_s \) is significantly greater than the adjacent areas (Nair et al., 2006). All the above observations can be explained by intrusion and underplating of mantle-derived materials into the crust (Nair et al., 2006), as well as refertilization of the lithosphere by the mafic intrusion oc-
curred at 2.05 Ga (de Wit et al., 1992; James et al., 2001; Jordan, 1979; Li & Burke, 2006; Schouwstra et al., 2000).

### 4.4 Lower Crustal Eclogitization Beneath the Limpopo Belt

Relative to the Kaapvaal craton, the Limpopo belt is characterized by a lower elevation (Figure 13a), thicker crust (Figure 11), and higher crustal shear wave velocities (Figure 12b). In contrast, another area with thick crust, the Proterozoic Namaqua-Natal mobile belt, has a higher elevation than the Kaapvaal craton (Figures 11 and 13), and a slightly higher crustal shear wave velocity (Figure 12). The counter-intuitive relationship between the lower elevation and thicker crust beneath the Limpopo belt can be explained by the existence of a high density, probably eclogitized lower crustal layer.

It has been recognized that the less dense gabbro (density=3.0 g/cm$^3$, $V_p=6.9$ km/s) in the lower continental crust can be transformed into more dense eclogite (density=3.5 g/cm$^3$, $V_p=7.9$-8.05 km/s) in tectonically over-thickened crust (e.g., Kay & Mahlburg-Kay, 1991; Kern et al., 1999; Ringwood, 1975). Such a eclogitized layer has been revealed in many regions in the world (e.g., Keller, 2013; Rumpfhuber & Keller, 2009). Bouguer gravity anomalies (Ranganai et al., 2002) are relatively higher in the Limpopo belt than the adjacent Zimbabwe and Kaapvaal cratons, providing independent evidence for the presence of a high density crustal layer.

### 4.5 A Possible Fossil Oceanic Slab Beneath the Southern Namaqua-Natal Mobile Belt

A high velocity anomaly is consistently present beneath the southern Namaqua-Natal Mobile Belt in the 50-100 km depth range (Figures 9e-9h). From the cross-section (Figure 10) and velocities at various depth ranges (Figure 12), it is clear that this feature extends from beneath the Moho to at least 100 km depth. One of the possible interpretations of this high velocity feature is a fossil oceanic slab beneath the suture zone with the Cape foldbelt to the south. The assimilation of the Cape foldbelt occurred during 800 - 1000 Ma and prior to the assimilation, there existed an oceanic plate (de Beer et al., 1982; Lock, 1980). Such high velocity belts in the lithosphere have been identified on the edges of other cratonic blocks (e.g., Bostock, 1997 for the Slave Craton).
5 Conclusions

Three-dimensional distributions of shear wave velocities in the top 100 km of the
lithosphere beneath two of the oldest cratons on Earth and orogenic belts of various ages
are revealed using ambient noise and earthquake surface wave tomography, with constraints
from P-to-S receiver functions. The observations provide constraints on a number of sig-
nificant problems regarding continental lithospheric structure and evolution. The unmod-
ified area of the Kaapvaal craton is characterized by high mantle velocities which are con-
sistent with the basalt removal for the formation of continental tectosphere. Crustal thick-
ening and higher crustal velocities beneath the SW Zimbabwe craton and the Bushveld
complex can be explained by magmatic intrusion and underplating, and the observed
lower velocity and higher density in the mantle lithosphere beneath the two magmat-
ically modified areas are most likely the results of mantle refertilization. While a thicker
crustal root is found to correspond with the higher elevation beneath the Proterozoic Namaqua-
Natal mobile belt, the thicker crust found beneath the lower elevation Archean Limpopo
belt is probably at least partially compensated by a high density lower crustal layer which
could be resulted from eclogitization of the gabbro-rich lower crust. We interpret a high-
velocity zone along the southern margin of the Namaqua-Natal mobile belt as a segment
of stalled oceanic lithosphere.

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Figure 1. An elevation map of the study area showing seismic stations used in the study (triangles) and major tectonic provinces. Stations along profile A-A’ (blue dashed line) are marked by the red triangles, and those without reliable receiver function measurements of crustal thickness are marked by red station names. The inset in the upper left corner is an azimuthal equidistant projection map centered at the study area showing the distribution of earthquakes used for receiver function (blue circles) and two-station surface wave dispersion (green circles) analyses. The rectangle area in the inset map in the lower right corner shows the location of the study area. BC, Bushveld complex; VC, Ventersdrop complex; MFC, Molopo Farms complex.
Figure 2. (a) Ray paths between Station SA38 (red triangle) and all the rest stations (green triangles). The thick red line in Zimbabwe represents the Great Dyke, and the green lines are the main branches of the Okavango Dyke Swarm (ODS) (Le Gall et al., 2002; Uken & Watkeys, 1997). (b) 2–40 s band-pass filtered cross-correlation functions between Station SA38 and the other stations.
Figure 3. $H - \kappa$ stacking of RFs from Station SA38. (a) RFs plotted against the back azimuth. The red trace is the result of simple time domain summation of the individual traces. (b) $H-\kappa$ stacking using the RFs in (a).
Figure 4. Four examples of initial models for the joint inversion. The black line represents initial S-wave model for Station SA38 in the Kaapvaal craton, red line is for Station SA47 in the Bushveld complex, green line is for Station SA55 in the Limpopo belt, and the blue line is for Station SA82 in the Namaqua-Natal mobile belt.
Figure 5. Rayleigh wave phase velocity maps from EFG (a-c) and two-station (e-i) analyses. (d) shows the difference between phase velocities from EFG and two-station analyses at the period of 24 s.
Figure 6. Averaged Rayleigh wave phase velocity curves over the entire study area from (a) EGF analysis, and (b) two-station analysis. (c) Combined result of phase velocity curves for the period range of 6 to 80 s. Note the consistency between the results from the two methods in the overlapping periods (20-30 s).
Figure 7. Horizontal checkerboard model (a) and its reconstructions (b-h) at different periods. The color bar in (a) represents velocities with both positive and negative 5% perturbations compared with a reference velocity of 4 km/s. (a) Target checkerboard model. (b)-(d) Recovered velocity results from the EGF analysis for the periods of 6, 16, and 24 s, respectively. (e)-(h) Recovered velocity results from the two-station analysis for the periods of 32, 40, 60, and 80 s, respectively.
Figure 8. Joint inversion results for stations SA38 (a-c) and SA55 (d-f). (a) Ensemble of accepted models using the joint inversion approach for Station SA38. The 1σ width of the ensemble is presented as light-gray curves enclosing the area between the two curves, and the average model is the red curve near the middle of the ensemble. The horizontal blue dash line indicates the crust thickness beneath the station. (b) Observed Rayleigh wave phase velocities (dots) and 1σ error bars for Station SA38. The red curve represents the prediction from the best fitting model in (a). (c) Stacked RF trace (black curve) and the 1σ uncertainty (light-gray curves) for Station SA38. The red curve is the predicted RF from the best fitting model in (a). (d)-(f) are the same as (a)-(c), but for Station SA55.
Figure 9. Horizontal shear wave velocity slices at different depths. (a) 6 km. (b) 20 km. (c) 30 km. (d) 40 km. (e) 50 km. (f) 60 km. (g) 80 km. (h) 100 km.
Figure 10. Vertical S-wave velocity cross-section from the surface to the depth of 100 km along Profile A-A’ in Figure 1. The crosses represent crustal thickness beneath the stations from the joint inversion method.
Figure 11. Crustal thickness measurements. (a) Results from the joint Bayesian Monte-Carlo inversion approach. (b) Results from $H - \kappa$ stacking of RFs. (c) Difference between results shown in (a) and (b). Red triangles represent stations within or close to the Bushveld complex, and green ones represent the rest of the stations within the Kaapvaal craton.
Figure 12. Mean shear wave velocities. (a) From the surface to 100 km depth. (b) From the surface to the Moho. (c) From the Moho to 100 km depth. (d) From 55 km to 100 km depth.
Figure 13. (a) Elevation variation along profile A-A'. (b) Variation of crustal thickness from joint inversion along profile A-A'. (c) Variation of mean shear wave velocities for 4 depth ranges.