An infinitely long insulating cylindrical shell has an inner radius $a$, an outer radius $b$, and an unknown uniform positive charge density $\rho$ (charge per unit volume) distributed in the region between $r=a$ and $r=b$.
(a) Using Gauss’s law, find the electric field in the hollow inner region $r<a$. Begin with a statement of Gauss's Law and justify all steps leading to your answer.

(b) Suppose the electric field at the outer edge of the cylindrical shell (i.e., at $r=b$ ) is measured, and is found to have a magnitude of $E_{0}$. Use Gauss's law to express the charge density $\rho$ in terms of the quantities $E_{0}, a, b$, and any fundamental constants you may need. Leave your answer in symbolic form.
(c) Find the magnitude $E$ of the electric field at a radial distance $a<r<b$ from the center of the cylindrical shell. Express your answer in terms of fundamental constants and some combination of $a, b, r, E_{0}$, and/or $\rho$.

