

1. Read Chapter 1 of the textbook.
2. Let the propositions  $p$ ,  $q$ ,  $r$ , and  $s$  be given as follows.  $p$  :  $1 + 3 = 5$ ;  $q$  :  $-1$  is the square of some real number;  $r$ : The capital of Liechtenstein is Vaduz;  $s$ : Sierra Nevada Beer is brewed in Chico, CA. Find the truth values for:
  - (a)  $p \vee q$ ;
  - (b)  $r \wedge s$ ;
  - (c)  $\overline{(p \vee q)} \wedge (\overline{r} \vee s) \wedge (\overline{p} \wedge s)$ ;
  - (d)  $(p \vee s) \wedge (q \vee r) \vee \overline{(r \vee s)}$ ;
  - (e)  $\overline{p \rightarrow q}$ ;
  - (f)  $(p \wedge r) \leftrightarrow r$ ;
  - (g)  $p \vee (\overline{p} \wedge \overline{(q \vee r)}) \rightarrow (p \vee \overline{(r \vee q)})$ .
3. Find the truth tables for
  - (a)  $(p \wedge q) \vee \overline{q}$ ;
  - (b)  $(p \vee q) \wedge \overline{(\overline{p} \vee q)}$ .
4. Work on problems 42–55 of Section 1.2 of the textbook.
5. Are the following statements true or false? Prove your claim.
  - (a)  $\forall x \in \mathbb{R} x^2 - 9 = 0$ ;
  - (b)  $\exists x \in \mathbb{R} x^2 - 9 = 0$ ;
  - (c)  $\forall x \in \mathbb{R} \exists y \in \mathbb{R} x = y^2$ ;
  - (d)  $\exists x \in \mathbb{R} \forall y \in \mathbb{R} xy = 0$ ;
  - (e)  $\forall \varepsilon > 0 \exists N \in \mathbb{N} \frac{1}{N} < \varepsilon$ ;
  - (f)  $\forall \varepsilon > 0 \exists \delta > 0 \forall x \in (0, \delta) x^2 \in (0, \varepsilon)$ .