- 1. Define the outer measure of a set $A \subset \mathbb{R}^N$.
- 2. The outer measure is monotone and subadditive. What does that mean?
- 3. When is a subset of \mathbb{R}^N called Lebesgue measurable?
- 4. Give five examples of classes of sets that are Lebesgue measurable.
- 5. If a set A is Lebesgue measurable, how can A^C be written?
- 6. Define in detail what a σ -algebra is.
- 7. Define in detail what a measure space is.
- 8. When is a measure space complete?
- 9. Give two examples of a measure space.
- 10. When is a function called measurable?
- 11. How did we define f^+ and f^- ? What are their relations to |f|?
- 12. When are two functions f and g said to be equal almost everywhere?
- 13. When is a function called summable?
- 14. Define the sets $A_{\infty}(f)$, $A_0(f)$, $A_{nk}(f)$ and the sums $s_n(f)$.
- 15. State the three main results on the sums s_n .
- 16. How is the integral of a summable function over X defined? How about over A?
- 17. What are the three consequences of #15 for integrals?
- 18. State the converse of the Radon-Nikodym theorem.
- 19. State the theorem of Beppo Levi (Monotone Convergence).
- 20. State Fatou's lemma.