

$$c(s, t) = sN(d_+(s, T - t)) - Ke^{-r(T-t)}N(d_-(s, T - t)), \quad d_{\pm}(s, \tau) = \frac{\ln\left(\frac{s}{K}\right) + \left(r \pm \frac{\sigma^2}{2}\right)\tau}{\sigma\sqrt{\tau}}.$$

(1)

$$d_-(s, \tau) = d_+(s, \tau) - \sigma\sqrt{\tau},$$

(2)

$$\frac{\partial d_+(s, T - t)}{\partial t} = \frac{\partial d_-(s, T - t)}{\partial t} - \frac{\sigma}{2\sqrt{T - t}},$$

(3)

$$\frac{\partial d_+(s, \tau)}{\partial s} = \frac{\partial d_-(s, \tau)}{\partial s} = \frac{1}{\sigma s\sqrt{\tau}},$$

(4)

$$N'(x) = \frac{1}{\sqrt{2\pi}}e^{-\frac{x^2}{2}},$$

(5)

$$sN'(d_+(s, \tau)) - Ke^{-r\tau}N'(d_-(s, \tau)) = 0,$$

(6)

$$\frac{\partial c(s, t)}{\partial t} = -rKe^{-r(T-t)}N(d_-(s, T - t)) - \frac{\sigma s}{2\sqrt{T - t}}N'(d_+(s, T - t)),$$

(7)

$$\frac{\partial c(s, t)}{\partial s} = N(d_+(s, T - t)),$$

(8)

$$\frac{\partial^2 c(s, t)}{\partial s^2} = \frac{N'(d_+(s, T - t))}{\sigma s\sqrt{T - t}},$$

(9)

$$\frac{\partial c(s, t)}{\partial t} + rs\frac{\partial c(s, t)}{\partial s} + \frac{\sigma^2 s^2}{2}\frac{\partial^2 c(s, t)}{\partial s^2} = rc(s, t),$$

(10)

$$\lim_{t \rightarrow T^-} c(s, t) = (s - K)^+.$$