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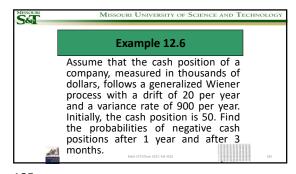
MISSOURI MISSOURI UNIVERSITY OF SCIENCE AND TECHNOLOGY **Definition 12.3** A stochastic process follows a Wiener process if • the change  $\Delta W$  during a small period of time Δt is  $\Delta W = \varepsilon (\Delta t)^{1/2}$ , where  $\varepsilon \sim N(0,1)$ ,  $\bullet$  the values of  $\Delta W$  for any two different short intervals of time  $\Delta t$ are independent.

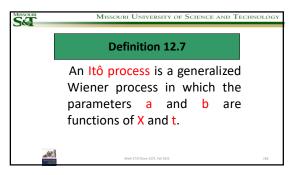
MISSOURI MISSOURI UNIVERSITY OF SCIENCE AND TECHNOLOGY Example 12.4 Suppose W follows a Wiener process and time is measured in years. Suppose the value of W is initially 25. What is the value of W at the end of one year? What is the value of W at the end of five years? Find P(W(1)>26) and P(W(5)>26).

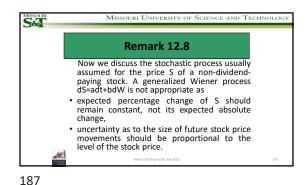
MISSOURI UNIVERSITY OF SCIENCE AND TECHNOLOGY MISSOURI **Definition 12.5** A stochastic process X follows a generalized Wiener process with drift rate a and variance rate b2 if dX=adt+bdW. where W is a Wiener process.

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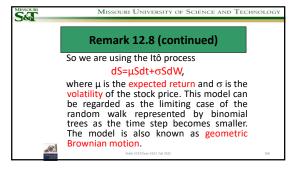
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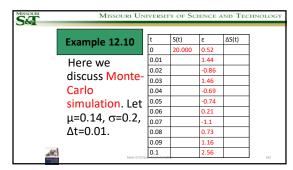


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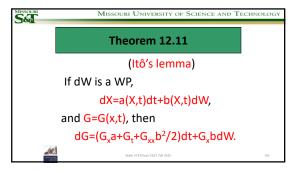


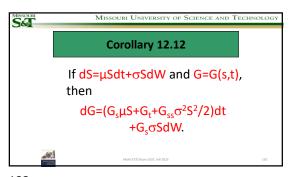
Example 12.9

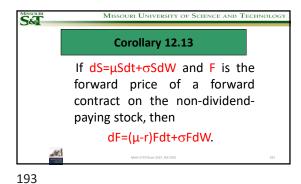
Consider a non-dividend-paying stock with volatility 30% (pa) providing expected return of 15%. Suppose the stock price is initially 100. Assuming the stock price follows GBM, what is the probability that the stock price after one week is more than 100?



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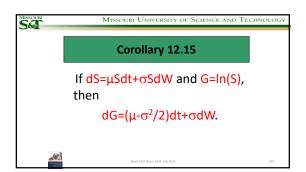




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Remark 12.14

Note that F in Corollary 12.13 follows again geometric Brownian motion with the same variance rate as the stock price and a growth rate equal to the excess return of the stock price over the risk-free rate.



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