

Chapter 3

Hedging Strategies using Futures



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23

23

Definition 3.1

- A **short hedge** is a hedge involving a short position in a futures contract
- A **long hedge** is a hedge involving a long position in a futures contract



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24

24

Remark 3.2

- Short hedges are appropriate when you know you will sell the asset in the future
- Long hedges are appropriate when you know you will buy the asset in the future



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25

25

Remark 3.2 (continued)

- Arguments for hedging: Minimizing risks arising from interest rates, exchange rates, and other market variables
- Arguments against hedging: Shareholders can do it themselves, risk may increase if competitors do not hedge, explaining a situation where there is a loss on the hedge and a gain on the underlying can be difficult



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26

26

Example 3.3

Assume a hedge is put in place at time 1 and closed out at time 2,

$$\begin{aligned} S_1 &= 2.50, & F_1 &= 2.20, \\ S_2 &= 2.00, & F_2 &= 1.90. \end{aligned}$$

If hedger knows that asset will be sold at time 2, what is the effective price that is obtained for the asset with hedging?



Definition 3.4

- **Cross hedging** occurs if the asset underlying the futures price is not the same as the asset whose price is being hedged.
- The **hedge ratio** is the ratio of the size of futures contracts to the size of shares of the underlying held.
- The **minimum variance hedge ratio** is the hedge ratio that results in the risk (measured by the variance) being minimal.



Theorem 3.5

$$h^* = \rho_{SF} \frac{\sigma_S}{\sigma_F}$$

where σ_S and σ_F are the standard deviations of ΔS and ΔF , respectively, and ρ_{SF} is the correlation coefficient between ΔS and ΔF .



Example 3.6

An airline expects to purchase 2 million gallons of jet fuel in one month and decides to use heating oil futures for hedging. One futures contract is on 42,000 gallons. It is given that the standard deviations of the changes in fuel price and in the futures price (per gallon) are 0.03 and 0.04, respectively, and the correlation coefficient between these two changes is 0.9.



Example 3.7

An airline expects to purchase 2 million gallons of jet fuel in one month and decides to use heating oil futures for hedging. One futures contract is on 42,000 gallons.



Example 3.7 (continued)

Month	Change in fuel price per gallon	Change in futures price per gallon			
1	0.029	0.021	8	-0.007	-0.029
2	0.020	0.035	9	0.043	0.048
3	-0.044	-0.046	10	0.011	-0.006
4	0.008	0.001	11	-0.036	-0.036
5	0.026	0.044	12	-0.018	-0.011
6	-0.019	-0.029	13	0.009	0.019
7	-0.010	-0.026	14	-0.032	-0.027
			15	0.023	0.029



Remark 3.8

A **stock index** tracks changes in the value of a hypothetical portfolio of stocks. Futures contracts on stock indices are settled in cash.



Remark 3.9

The **beta** of a portfolio is defined by

$$\beta_V = \rho_{VM} \frac{\sigma_V}{\sigma_M}$$

and it satisfies (Capital Asset Pricing Model)

$$\beta_V = \frac{\mu_V - r_F}{\mu_M - r_F}.$$



Example 3.10

We assume now:

- Value of S&P500 index: 1000
- Value of portfolio: 5,000,000
- Beta of portfolio: $\beta = 1.5$
- One futures contract is \$1010 and for delivery of 250 times the index

