

Nicely show all your work on this page. No books, notes, calculators!

1. Let  $f(x) = \frac{x^2-16}{2x-2}$ . Is  $f$  symmetric? Find the domain of  $f$ , the  $x$  and  $y$  intercepts, the asymptotes, the intervals where  $f$  is increasing, decreasing, concave upwards, and concave downwards, respectively, the local extrema, the inflection points, and sketch the graph of  $f$ .
2. Party. You are at the point  $(0, 1)$ , the bar is the interval  $[0, 1]$  on the  $x$ -axis. Suddenly you see your neighbor who is standing at  $(1, 2)$ . You want to go to talk to him, but first go to the point  $(p, 0)$  at the bar and grab a drink (i.e., go straight from  $(0, 1)$  to  $(p, 0)$  and then straight from  $(p, 0)$  to  $(1, 2)$ ). Draw a picture of the scene and describe the travel distance as a function of  $p$ . How long is the minimal (in case your neighbor is a good friend) and the maximal (in case your neighbor isn't such a good friend) travel distance?
3. Graph the function  $f(x) = x^2 + 2x + 1$ . Use Newton's method with  $x_0 = 0$  to calculate (and plot)  $x_1, x_2, x_3, x_4$ . Give a formula for  $x_n$ . What is the limit of  $x_n$  as  $n \rightarrow \infty$ ?