Math 15, Exam 4, Apr 27, 2006

Instructions

Calculators may be used on this exam.

However, you must show your work in order to receive credit.

- 1. Be sure to print your name and your instructor's name in the space provided.
- 2. Work all problems. Show all work. Full credit will be given only if work is shown which fully justifies your answer.
- 3. There will be sufficient space under each problem in which to show your work.
- 4. Circle, box, or underline each final answer. All final answers must be simplified!
- 5. This exam has 4 sheets of paper (front and back). Do not remove the staple! There are 100 points. Each problem is 10 points.
- 6. Turn off your cell phone if you have one with you.

Get ready for the exam

- 1. Some formulas will be supplied (see below). You are asked to remember other formulas and techniques from Chapters 7-12 and Math 14.
- 2. Problems will be (directly or slightly modified) from homework problems assigned from Section 8.7 and Chapters 9-11.
- 3. You should be able to do all of the following:
 - a. Use the Midpoint, Trapezoidal, and Simpson rules.
 - b. Find the length of an arc.
 - c. Calculate force due to liquid pressure and find the centroid of a planar figure.
 - d. Check whether a given function is a pdf, find the mean and related probabilities.
 - e. Check whether certain functions are solutions of given differential equations.
 - f. Solve problems of exponential growth or decay such as bacteria growth, radioactive decay, Newton's law of cooling, and continuously compounded interest.
 - g. Sketch curves given in parametric form and find tangent lines to such curves.
 - h. Find arc length and areas using equations in parametric form.

$$S_n = \frac{\Delta x}{3} \left[f(x_0) + 4f(x_1) + 2f(x_2) + 4f(x_3) + \dots + 2f(x_{n-2}) + 4f(x_{n-1}) + f(x_n) \right]$$

$$T_n = \frac{\Delta x}{2} \left[f(x_0) + 2f(x_1) + 2f(x_2) + \dots + 2f(x_{n-1}) + f(x_n) \right]$$

$$M_{y} = \rho \int_{a}^{b} x [f(x) - g(x)] dx \qquad \qquad M_{x} = \rho \int_{a}^{b} \frac{1}{2} \left[(f(x))^{2} - (g(x))^{2} \right] dx$$

$$\bar{x} = \frac{M_y}{m} \qquad \bar{y} = \frac{M_x}{m} \qquad m = \rho A$$
$$L = \int_a^b \sqrt{1 + \left(\frac{dy}{dx}\right)^2} dx \qquad L = \int_c^d \sqrt{1 + \left(\frac{dx}{dy}\right)^2} dy$$

