- 59. Show that  $K \leq K'$  and  $0 < \alpha < 1$  imply  $p(\alpha K + (1 \alpha)K') \leq \alpha p(K) + (1 \alpha)p(K')$ .
- 60. Calculate and draw a bull put spread's profit function.
- 61. Use put-call parity to relate the initial investment for a bull spread created using calls to the initial investment for a bull spread created using puts.
- 62. Suppose that put options on a stock with strike prices \$30 and \$35 cost \$4 and \$7, respectively. How can the options be used to create (a) a bear spread and (b) a bull spread? Graph the profit function for both spreads.
- 63. Three put options on a stock have the same expiration date and strike prices of \$55, \$60, and \$65 and market prices \$3, \$5, and \$8. Explain how a butterfly spread can be created. Graph the profit function from the strategy. For what range of stock prices would the butterfly spread lead to a loss?
- 64. Draw graphs showing the variation of an investor's profit and loss with terminal stock price for a portfolio consisting of:
  - (a) One share and a short position in one call option.
  - (b) One share and a short position in two call options.
  - (c) One share and a short position in four call options.
  - (d) Two shares and a short position in one call option.

In each case, assume that the call option has an exercise price equal to the current stock price.

- 65. Use put-call parity to show that the cost of a butterfly spread created from European puts is identical to the cost of a butterfly spread created from European calls.
- 66. A call option with a strike price of \$50 costs \$2. A put option with a strike price of \$45 costs \$3. Explain how a strangle can be created from these two options. What is the graph of the profits function from the strangle?