

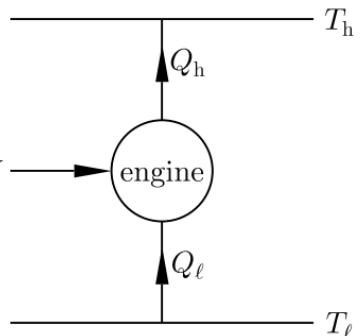
Physics 4311: Thermal Physics - Homework 6

due date: Tuesday, March 7, 2023, please upload your solution as a pdf on Canvas

Problem 1: Heat pump (16 points)

A heat pump is a device that uses work to transport heat from a low-temperature reservoir to a high-temperature reservoir (see figure on the right). Its efficiency can be defined as the ratio of the heat deposited into the high-temperature reservoir and the work done on the system, $\eta = |Q_h|/W$.

- Consider a heat pump consisting of a Carnot engine running backwards. Using the results for the ideal-gas based Carnot engine discussed in class, find the efficiency of this “ideal” heat pump in terms of T_h and T_l .
- Is the efficiency larger or smaller than unity? Explain what the result means.
- Heat pumps can be used to heat buildings. What is the efficiency of an ideal (Carnot) heat pump that takes heat from the outside air at 50 °F and transports it to the inside of the building which is at 70 °F?
- What is the efficiency of the heat pump in part c) if the outside air is at a temperature of 10 °F?



Problem 2: Carnot process for a dielectric substance (24 points)

Consider a dielectric substance whose equation of state reads $P = \alpha E/T$ where T is the temperature, P is the polarization, E is electric field, and α is a material specific constant. The internal energy is given by $U = CT$ where the specific heat C is a constant. The work differential for a dielectric is $\delta W = EdP$

- Consider an isothermal change of polarization from P_1 to P_2 . Compute the work W_{12} done on the system and the heat Q_{12} absorbed by the system.
- Consider an adiabatic change of polarization from P_2 to P_3 . Find the adiabatic $E - P$ curves by starting from $\delta Q = 0$ and integrating the resulting differential equation.
- Sketch a Carnot cycle, consisting of two isothermal changes in P and two adiabatic changes in P in the $P - E$ plane.
- Compute the total absorbed heat and the work during the four segments of the cycle.
- Explicitly calculate the efficiency.

Hint: The derivation is analogous to that of the Carnot cycle for the ideal gas, but using the equation of state $P = \alpha E/T$ instead of the ideal gas law. This leads to changes in some of the mathematical expressions.