Physics 481: Condensed Matter Physics - Homework 9

due date: Friday, March 25, 2011

Problem 1: Copper nanowire (20 points)

Consider a long thin wire of copper along the z-direction with length L = 1 cm and a square cross section (width a is a few Å). Treat the wire as a free electron gas, demanding that the wave function vanishes outside of the wire. Use periodic boundary conditions along the length of the wire. The electron density for copper is 8.49×10^{22} electrons/cm³.

- a) Solve the Schrödinger equation for this geometry.
- b) Which states are occupied at zero temperature? Qualitatively describe the dependence on the width a.
- c) Calculate the maximum possible width a of the wire such that only the ground state in x and y directions is occupied.
- d) Calculate the low-temperature specific heat for the case when only the ground state in x and y directions is occupied (algebraic answer in terms of a and the electron density OK).

Problem 2: Electronic density of states (10 points)

Calculate the electronic density of states of the free electron gas in one and two spatial dimensions. Discuss the character of the van-Hove singularity at $\epsilon = 0$ in these cases.

Problem 3: Pressure of ideal Fermi gas (Marder, problem 6.3, 10 points)

Find the pressure of the free electron gas in three dimensions at zero temperature. Hint: Start from a thermodynamic relation, e.g., $p = -(\partial E/\partial V)_N$ (at zero temperature).